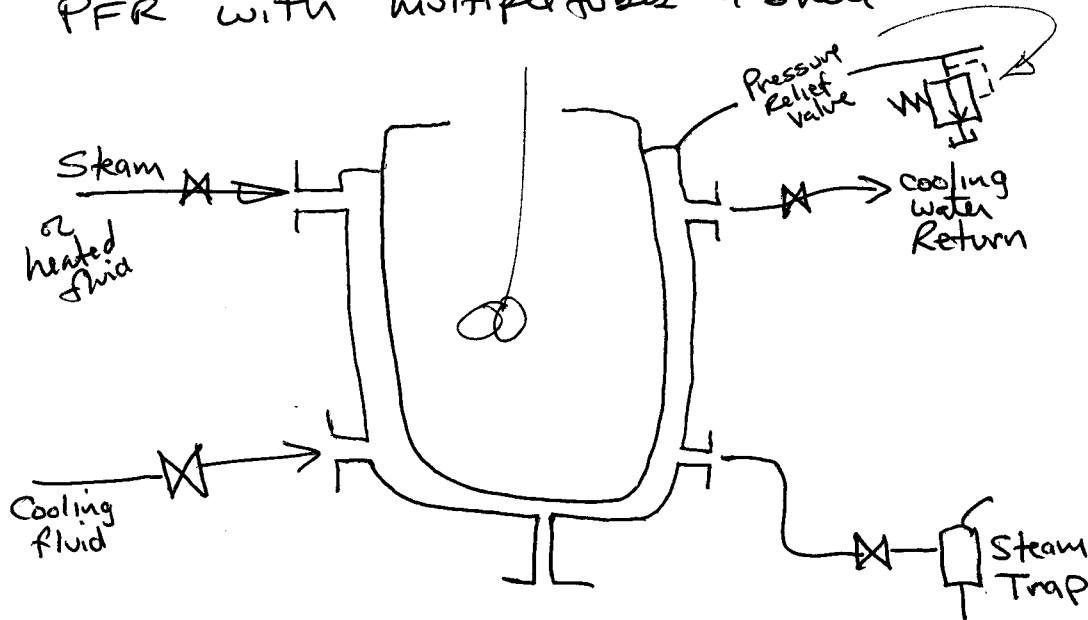


# Chapter 8

Show pictures of

CSTR with jacket

PFR with multiple tubes & shell



Typical values for steam heating of water

$$u = 70 \text{ Btu/hr ft}^2 \text{ } ^\circ\text{F} \quad \text{water}$$

90 RPM

$$u = 55 \text{ Btu/hr ft}^2 \text{ } ^\circ\text{F} \quad \text{Toluene}$$

Best scenario is to use a <sup>single</sup> heat transfer fluid for both heating and cooling

Dowtherm  $-80 - 315^\circ\text{C}$  or  $15 - 400^\circ\text{C}$

Syltherm  $-160 - 260^\circ\text{C}$

Typical values for shell & tube - see Perry's

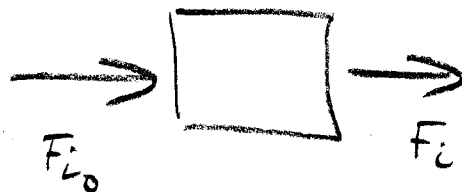
What happens if we use saturated steam?

at 30 psia  $250^\circ\text{F}$   
 15 psia ~~212~~  $212^\circ\text{F}$  (atmospheric)

this keeps a constant temperature in jacket.

## ch 8

Why do we need a detailed E bal?

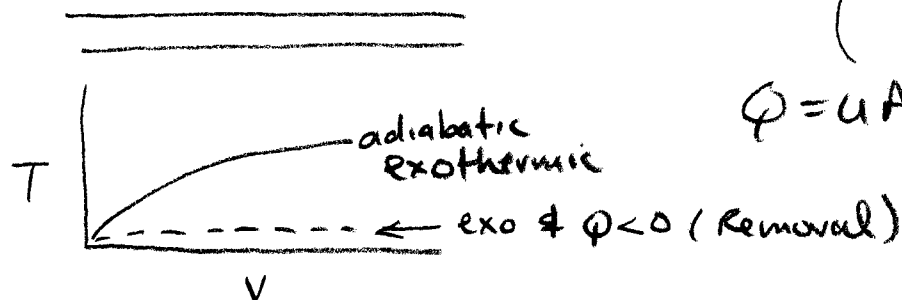


overall mol balance  $\chi = \frac{F_{i0} - F_i}{F_{i0}}$

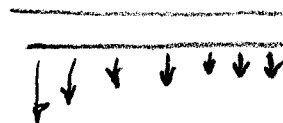
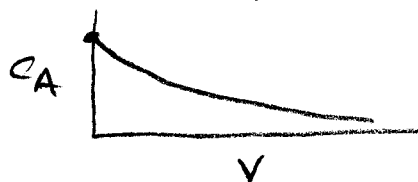
overall E balance

$$0 = \sum F_{i0} H_{i0} - \sum F_i H_i + \dot{Q}$$

heat in as positive



$$\dot{Q} = UA(T_a - T)$$



$$r = -kC_A$$

$$k = A \exp(-E/RT)$$

from E Bal

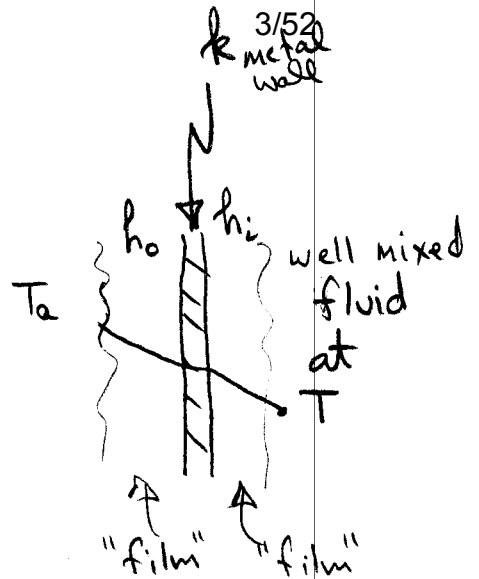
# Chapter 8 -

heat added by jacket

CASE I  $\dot{Q} = U_i A_i (T_a - T)$  (8-34)

$$\frac{1}{U_i} = \frac{1}{h_i} + \frac{\Delta x A_i}{k A_o} + \frac{1}{h_o} \frac{A_i}{A_o}$$

- $\Delta T_a \approx 0$
- ① fast flow of liquid
  - ② condensing steam

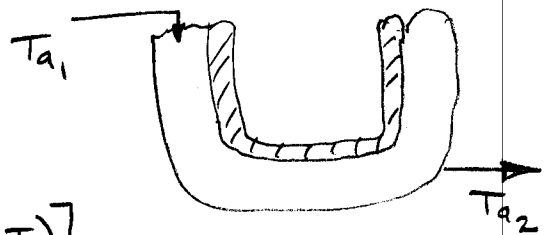


CASE II

If  $T_a$  changes then use a  $\Delta T_{em}$

$$\dot{Q} = U A_i \Delta T_{em}$$

(8-35) 
$$\Delta T_{em} = \frac{T_{a1} - T_{a2}}{\ln \left[ \frac{T_{a1} - T}{T_{a2} - T} \right]}$$



8-61

$$V \sum_{i=1}^n C_{p_i} C_i \frac{dT}{dt} = \dot{Q} - \dot{W}_s - F_{A0} \sum_{i=1}^n \frac{F_{i0}}{F_{A0}} C_{p_i} (T - T_{i0}) - \Delta H_{rxn} (-r_A V)$$

for more than one reaction

$$\sum_{j=1}^m \Delta H_{rxn_j} (-r_j V)$$



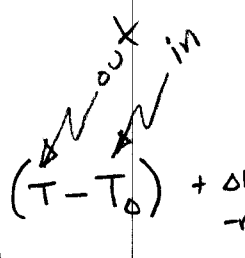
- ① Assume that  $C_{A0} \neq 0 \neq C_{B0} \neq 0$   $C_{C0} = 0$
- ② Same T

$$C_{A0} C_{B0} C_{C0} = 0$$

$$C_{A_i} = C_{B_i} = 0 \quad t=0$$

$$V [C_{p_A} C_A + C_{p_B} C_B + C_{p_C} C_C] \frac{dT}{dt}$$

$$= U_i A_i (T_a - T) - \dot{W}_s - F_{A0} \left[ \frac{F_{A0}}{F_{A0}} C_{p_A} + \frac{F_{B0}}{F_{A0}} C_{p_B} + \frac{F_{C0}}{F_{A0}} C_{p_C} \right] (T - T_0) + \Delta H_{rxn} (-r_A V)$$



But Remember definitions

$$\sum C_{P_i} \equiv \frac{\int_{T_0}^T C_{P_i} dT}{T - T_0}$$

↑ entering +1010  
Temperature

(fluidized bed) Highly exothermic  
fixed bed:  $\Delta H = -40 \frac{\text{kcal}}{\text{mol}}$

AND

$$\Delta H_{\text{rxn}}|_T = \Delta H_{\text{rxn}}|_{T_R} + \Delta \hat{C}_p (T - T_R) \quad (8-27)$$

per mole or kg of A.      Reference temperature (eg.  $T_R = 298 \text{ K}$  or  $20^\circ \text{C}$ )

must be the same

$$\Delta \hat{C}_p \equiv \frac{\int_{T_R}^T \Delta C_p dT}{T - T_R}$$

$$\Delta C_p \equiv \frac{d}{a} C_{p_D} + \frac{c}{a} C_{p_C} - \frac{b}{a} C_{p_B} - \frac{a}{a} C_{p_A}$$

↑  
per mole or kg of A!

Don't forget to include any  $\Delta H_{\text{melting}}$  or  $\Delta H_{\text{vaporization}}$ !  
See example 8-2

$$\Delta H_{\text{rxn}}^0|_{T_R} \rightarrow \text{See } \underline{8-24}$$

effect on P see bottom of page 391!

**Energy Balance Derivations**

Evaluating the work term: 8.2.2: The work term is given by flow work plus mechanical work:

$$\dot{W} = -\sum_{i=1}^n F_i PV \Big|_{in} + \sum_{i=1}^n F_i PV \Big|_{out} + \dot{W}_s \quad (1)$$

**CSTR Energy Balance**

Control Volume: Fluid inside the reactor

Assumptions: The fluid is perfectly mixed - temperature of fluid is uniform

1) No  $\Delta H_{rxn}$   
2)  $c_p$ 's are integral averages

Mole Balance:

$$\frac{dN_i}{dt} = F_{i0} - F_i + \frac{v_i}{-a} r_A V \quad \text{E.B.} \quad (2)$$

The steady-state mole balance is:

$$F_i = F_{i0} + \frac{v_i}{-a} r_A V \quad \text{m.B.} \quad (3)$$

Energy Balance:

Accumulation = in - out + generation

$$\frac{dHN}{dt} = \sum_{i=1}^n H_{i0} F_{i0} - \sum_{i=1}^n H_i F_i + \dot{Q} - \dot{W}_s \quad (4)$$

} Basic Balance - same form as Felder

For steady-state operation:

$$0 = \sum_{i=1}^n H_{i0} F_{i0} - \sum_{i=1}^n H_i F_i + \dot{Q} - \dot{W}_s \quad (5)$$

Using a mean heat capacity,  $\tilde{C}_{pi}$ , of species  $i$  between temperature  $T_0$  and temperature  $T$

$T_0$  is inlet reactor feed Temp.

$$\tilde{C}_{pi} \equiv \frac{\int_{T_0}^T c_{pi} dT}{T - T_0}$$

} Definition given on Exam Page

the species enthalpy can be defined as

$$H_i = H_{i0} + \tilde{C}_{pi} (T - T_0) \quad (7)$$

Inserting the enthalpy defined by equation 7 and the steady-state mole balance of equation 3 yields:

$$0 = \sum_{i=1}^n H_{i0} F_{i0} - \sum_{i=1}^n \left( H_{i0} + \tilde{C}_{pi} (T - T_0) \right) \left( F_{i0} + \frac{v_i}{-a} r_A V \right) + \dot{Q} - \dot{W}_s \quad (8)$$

Multiply out terms

$$0 = \sum_{i=1}^n H_{i0} F_{i0} - \sum_{i=1}^n H_{i0} F_{i0} - \sum_{i=1}^n \left( F_{i0} \tilde{C}_{pi} (T - T_0) \right) + \sum_{i=1}^n \left( \frac{v_i}{a} H_{i0} + \frac{v_i}{a} \tilde{C}_{pi} (T - T_0) \right) (r_A V) + \dot{Q} - \dot{W}_s \quad (9)$$

Using the definition of the heat of reaction,  $\Delta H_{rxn}|_{T_0}$ , and an overall change in heat capacity,  $\Delta \tilde{C}_p$ ,

$$\Delta H_{rxn}|_{T_0} = \frac{d}{a} H_D|_{T_0} + \frac{c}{a} H_C|_{T_0} - \frac{b}{a} H_B|_{T_0} - H_A|_{T_0} = \sum_{i=1}^n \frac{v_i}{a} H_i|_{T_0}$$

with

$$\Delta \tilde{C}_p = \frac{d}{a} \tilde{C}_{pD} + \frac{c}{a} \tilde{C}_{pC} - \frac{b}{a} \tilde{C}_{pB} - \tilde{C}_{pA} = \sum_{i=1}^n \frac{v_i}{a} \tilde{C}_{pi} \quad (10)$$

the CSTR energy balance is:

$$0 = -\sum_{i=1}^n \left( F_{i0} \tilde{C}_{pi} (T - T_0) \right) + \left( \Delta H_{rxn}|_{T_0} + \Delta \tilde{C}_p (T - T_0) \right) (r_A V) + \dot{Q} - \dot{W}_s \quad (11)$$

and finally using the heat of reaction at the fluid temperature,  $\Delta H_{rxn}|_T$

group  $\Delta H_{rxn}|_T$

$$\Delta H_{rxn}|_T = \Delta H_{rxn}^\circ|_{T_0} + \Delta \tilde{C}_p (T - T_0)$$

gives the following steady-state mole balance for a CSTR:

$$0 = -\sum_{i=1}^n \left( F_{i0} \tilde{C}_{pi} (T - T_0) \right) + \left( \Delta H_{rxn}|_T \right) (r_A V) + \dot{Q} - \dot{W}_s \quad (12)$$

$$0 = F_{A0} - F_A + r_A V$$

$F_{A0} \times -F_A \times = +r_A V$

Now it is eqn 8-48

- 1) Show that balance has no  $\Delta H_{rxn}$  6/52
- 2) Define  $\Delta H_{rxn}$
- 3) Cp's are raw data & not averages

**Energy Balance Derivation: PFR**

Control Volume: a small cylindrical volume of fluid (plug)  $\Delta V$

Assumptions: There are no gradients of  $T, P,$  and  $C_i$  within the control volume with respect to  $r$  and  $\theta$ .

Mole Balance: 
$$\frac{\partial C_i}{\partial t} = -\frac{\partial F_i}{\partial V} + \frac{v_i}{-a} r_A \tag{1}$$

The steady-state mole balance is:

$$\frac{dF_i}{dV} = \frac{v_i}{-a} r_A \tag{2}$$

Energy Balance:

Accumulation = in - out + generation

Balance 
$$\frac{d\overline{HC}}{dt} \Delta V = \sum_{i=1}^n H_i F_i \Big|_V - \sum_{i=1}^n H_i F_i \Big|_{V+\Delta V} + \dot{q} \Delta V - \dot{w}_s \Delta V \tag{3}$$

divide by  $\Delta V$  
$$\frac{d\overline{HC}}{dt} = \frac{-\left(\sum_{i=1}^n H_i F_i \Big|_{V+\Delta V} - \sum_{i=1}^n H_i F_i \Big|_V\right)}{V + \Delta V - V} + \dot{q} - \dot{w}_s \tag{4}$$

$\lim_{\Delta V \rightarrow 0}$  
$$\lim_{\Delta V \rightarrow 0} \left[ \frac{d\overline{HC}}{dt} = \frac{-\left(\sum_{i=1}^n H_i F_i \Big|_{V+\Delta V} - \sum_{i=1}^n H_i F_i \Big|_V\right)}{V + \Delta V - V} + \dot{q} - \dot{w}_s \right] \tag{5}$$

Final Equation

$$\frac{\partial \overline{HC}}{\partial t} = \frac{-\partial \left( \sum_{i=1}^n H_i F_i \right)}{\partial V} + \dot{q} - \dot{w}_s \tag{6}$$

No  $\Delta H_{rxn}$

SS For steady-state operation:

mistake 
$$\frac{d \left( \sum_{i=1}^n H_i F_i \right)}{dV} = \dot{q} - \dot{w}_s \tag{7}$$

No  $\Delta H_{rxn}$

Using the chain rule:

$$\sum_{i=1}^n \left[ H_i \frac{dF_i}{dV} + F_i \frac{dH_i}{dV} \right] = \dot{q} - \dot{w}_s \tag{8}$$

put in mole balance for each species

Substituting the steady-state mole balance from equation 2 into the heat balance to eliminate  $\frac{dF_i}{dV}$

now we have a reaction term

$$\sum_{i=1}^n \left[ H_i \frac{v_i}{-a} r_A + F_i \frac{dH_i}{dV} \right] = \dot{q} - \dot{w}_s \tag{9}$$

$$\sum_{i=1}^n \left[ F_i \frac{dH_i}{dV} \right] = \sum_{i=1}^n \left[ H_i \frac{v_i}{-a} r_A \right] + \dot{q} - \dot{w}_s \tag{10}$$

Starting to look familiar

Using the definition of the heat of reaction,  $\Delta H_{rxn}|_T$

$$\Delta H_{rxn}|_T = \frac{d}{a} H_D|_T + \frac{c}{a} H_C|_T - \frac{b}{a} H_B|_T - H_A|_T = \sum_{i=1}^n \frac{\nu_i}{a} H_i|_T \quad (11)$$

$$\sum_{i=1}^n \left[ F_i \frac{dH_i}{dV} \right] = \Delta H_{rxn}|_T r_A + \dot{q} - \dot{w}_s \quad (12)$$

Substituting the definition of the enthalpy:  $H_i = C_{pi} T$

$$\sum_{i=1}^n [F_i C_{pi}] \frac{dT}{dV} = \Delta H_{rxn}|_T r_A + \dot{q} - \dot{w}_s \quad (13)$$

Substituting in for the molar flowrate of species  $i$  defined from chemical equation stoichiometry:

$$8-35 \quad \frac{dT}{dV} = \frac{\Delta H_{rxn} r + \dot{q}}{\sum F_i C_{pi}} \Rightarrow \frac{dT}{dV} = \frac{\Delta H_{rxn}|_T r_A + \dot{q} - \dot{w}_s}{\sum_{i=1}^n \left[ \left( F_{i0} + \frac{\nu_i}{a} F_{A0} \chi_A \right) C_{pi} \right]} \quad (14)$$

And using Foglers notation for the the change in heat capacity,  $\Delta C_{pi}$ ,

$$\text{with} \quad \Delta C_p = \frac{d}{a} C_{pD} + \frac{c}{a} C_{pC} - \frac{b}{a} C_{pB} - C_{pA} = \sum_{i=1}^n \frac{\nu_i}{a} C_{pi} \quad (15)$$

$$\frac{dT}{dV} = \frac{\Delta H_{rxn}|_T r_A + \dot{q} - \dot{w}_s}{\sum_{i=1}^n F_{i0} C_{pi} + \Delta C_p F_{A0} \chi_A} \quad (16)$$

This is the Fogler equation similar to 8-54 (In form)

Standard definition Equation 8-27

$$\Delta H_{rxn}|_T = \Delta H_{rxn}^{\circ}|_{T_R} + \Delta \hat{C}_p (T - T_R)$$

Note that this term will have some sort of integral average

$$\hat{C}_p \equiv \frac{\int_{T_R}^T C_p dT}{T - T_R}$$

alternative

$\Delta H_{rxn}|_T$  definition

look at  $C_p$ 's they are not integral averages

**ENERGY BALANCE Derivations: Batch Reactors:**

Control Volume: Fluid inside the reactor

Assumptions: The fluid is perfectly mixed - temperature of fluid is uniform

Mole Balance: 
$$\frac{dN_i}{dt} = \frac{v_i}{-a} r_A V \quad (1)$$

Energy Balance:

Accumulation = in - out + generation

*Basic Balance* 
$$\frac{d\overline{EN}}{dt} = \frac{d(\overline{U} + \overline{KE} + \overline{PE})\overline{N}}{dt} = \dot{Q} - \dot{W} \quad (2)$$

For most chemical reactor situations the kinetic,  $\overline{KE}$ , and potential energy,  $\overline{PE}$ , terms are negligible compared to the internal energy term,  $\overline{U}$ . In addition, the internal energy is given by

$$\overline{U} = \overline{H} - PV \quad (3)$$

Two derivations are given below; one for liquids and the other for gases.

**Liquid Derivation:**

For liquids the internal energy is approximately equal to the enthalpy  
~~Substituting equation 13 and assuming that the internal energy is equal to the total energy yields:~~  
**Great Assumption:**  $\overline{U} \approx \overline{H}$  *Batch Reactors (closed systems)*

Substituting equation 13 and assuming that the internal energy is equal to the total energy yields:

**B** 
$$\frac{d}{dt}[\overline{HN}] = \frac{d}{dt} \left[ \sum_{i=1}^n N_i H_i \right] = \sum_{i=1}^n \left[ H_i \frac{dN_i}{dt} + N_i \frac{dH_i}{dt} \right] = \dot{Q} - \dot{W}_s \quad (5)$$

Using the batch reactor mole balance, equation (1), into equation (5) to eliminate  $\frac{dN_i}{dt}$  gives:

$$\sum_{i=1}^n \left[ \left( \frac{v_i}{-a} r_A V \right) H_i + N_i \frac{dH_i}{dt} \right] = \dot{Q} - \dot{W}_s \quad (6)$$

$$\sum_{i=1}^n \left[ N_i \frac{dH_i}{dt} \right] = \sum_{i=1}^n \left[ \left( \frac{v_i}{a} r_A V \right) H_i \right] + \dot{Q} - \dot{W}_s = \sum_{i=1}^n \left( \frac{v_i}{a} H_i \right) r_A V + \dot{Q} - \dot{W}_s \quad (7)$$

The definition of the heat of reaction at a temperature,  $T$ , is:

$$\Delta H_{rxn}|_T = \frac{d}{a} H_D|_T + \frac{c}{a} H_C|_T - \frac{b}{a} H_B|_T - H_A|_T = \sum_{i=1}^n \frac{v_i}{a} H_i|_T \quad (8)$$

$$\sum_{i=1}^n \left[ N_i \frac{dH_i}{dt} \right] = \Delta H_{rxn}|_T r_A V + \dot{Q} - \dot{W}_s \quad (9)$$

Since  $H_i = C_{pi} T$  and from the stoichiometric table  $N_i = N_{i0} + \frac{v_i}{a} N_{A0} \chi_A$

$$\sum_{i=1}^n \left[ C_{pi} \left( N_{i0} + \frac{v_i}{a} N_{A0} \chi_A \right) \right] \frac{dT}{dt} = \Delta H_{rxn}|_T r_A V + \dot{Q} - \dot{W}_s \quad (10)$$

Using Foglers notation:

$$\sum_{i=1}^n [C_{pi} N_{i0} + \Delta C_p N_{A0} \chi_A] \frac{dT}{dt} = \Delta H_{rxn}|_T r_A V + \dot{Q} - \dot{W}_s \quad (11)$$

with

$$\Delta C_p = \frac{d}{a} C_{pD} + \frac{c}{a} C_{pC} - \frac{b}{a} C_{pB} - C_{pA} \quad (12)$$

*Batch equation*

*Do the type same things*



## Gas Derivation

For gases the internal energy is given by equation 3 and substituting the ideal gas law yields:

$$\bar{U} = \bar{H} - P\bar{V} = \bar{H} - RT \quad (13)$$

Substituting equation 13 into equation 5 and assuming that the internal energy is equal to the

Using the batch reactor mole balance, equation (1), into equation (14) to eliminate  $\frac{dN_i}{dt}$  gives:

$$\sum_{i=1}^n \left[ \left( \frac{v_i}{-a} r_A V \right) (H_i - RT) + N_i \frac{dH_i}{dt} - RN_i \frac{dT}{dt} \right] = \dot{Q} - \dot{W}_s \quad (15)$$

$$\sum_{i=1}^n \left[ N_i \frac{dH_i}{dt} - RN_i \frac{dT}{dt} \right] = \sum_{i=1}^n \left( \frac{v_i}{a} (H_i - RT) \right) r_A V + \dot{Q} - \dot{W}_s \quad (16)$$

The definition of the heat of reaction at a temperature,  $T$ , is:

$$\Delta H_{rxn}|_T = \frac{d}{a} H_D|_T + \frac{c}{a} H_C|_T - \frac{b}{a} H_B|_T - H_A|_T = \sum_{i=1}^n \frac{v_i}{a} H_i|_T \quad (17)$$

$$\sum_{i=1}^n \left[ N_i \frac{dH_i}{dt} \right] = \Delta H_{rxn}|_T r_A V + \sum_{i=1}^n \left( -RT \frac{v_i}{a} \right) r_A V + \dot{Q} - \dot{W}_s \quad (18)$$

Since  $H_i = C_{pi}T$  and from the stoichiometric table  $N_i = N_{i0} + \frac{v_i}{a} N_{A0} \chi_A$

$$\sum_{i=1}^n \left[ \left( C_{pi} - R \right) \left( N_{i0} + \frac{v_i}{a} N_{A0} \chi_A \right) \right] \frac{dT}{dt} = \Delta H_{rxn}|_T r_A V + \sum_{i=1}^n \left( -RT \frac{v_i}{a} \right) r_A V + \dot{Q} - \dot{W}_s \quad (19)$$

Using Foglers notation:

$$\sum_{i=1}^n \left[ C_{vi} N_{i0} + \Delta C_v N_{A0} \chi_A \right] \frac{dT}{dt} = \Delta H_{rxn}|_T r_A V + \sum_{i=1}^n \left( -RT \frac{v_i}{a} \right) r_A V + \dot{Q} - \dot{W}_s \quad (20)$$

with

$$\Delta C_v = \frac{d}{a} C_{vD} + \frac{c}{a} C_{vC} - \frac{b}{a} C_{vB} - C_{vA} \quad (21)$$

or using only internal energy instead of enthalpy:

$$\sum_{i=1}^n \left[ C_{vi} N_i \right] \frac{dT}{dt} = \Delta U_{rxn}|_T r_A V + \dot{Q} - \dot{W}_s \quad (22)$$

with the internal energy form of the heat of reaction given by:

$$\Delta U_{rxn}|_T = \Delta H_{rxn}|_T - \sum_{i=1}^n \left( RT \frac{v_i}{a} \right) \quad (23)$$

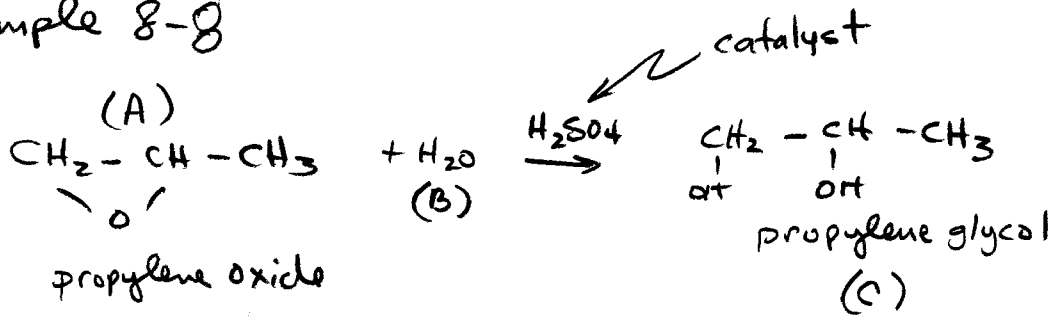
If the net change in the number of moles is equal to zero, then

$$\Delta U_{rxn}|_T = \Delta H_{rxn}|_T \quad (24)$$

Key Point:  
for a batch reactor  
energy Balance there is  
a difference between  
a gas & liquid

Steady-state CSTR

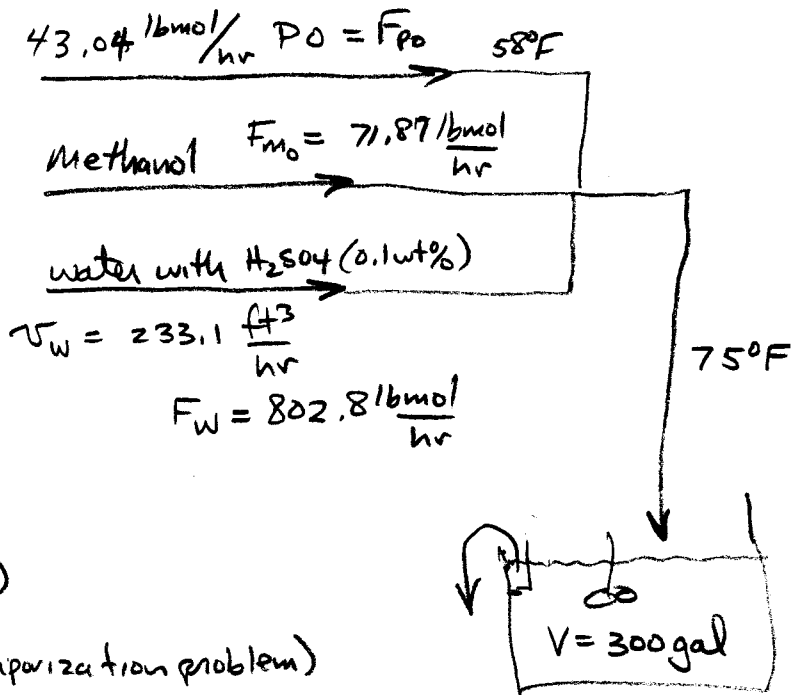
Example 8-8



Need new reactor - old one is leaking  
 - Overflow 300 gal reactor available (glass lined)

$V_{Po} = 46.62 \frac{\text{ft}^3}{\text{hr}}$

$V_M = 46.62 \frac{\text{ft}^3}{\text{hr}}$



$k = A \exp(-E/RT)$

$T < 125^\circ\text{F}$  (vaporization problem)

$460 + 125 = 585\text{R}$

can you use CSTR? - adiabatic?

ONLY V GIVEN  $X \neq T$  are unknown  $\left\{ \text{case B page 442} \right.$

$r_A = -k C_{Po}$

$X_{MB} = f(T) \text{ and } V$

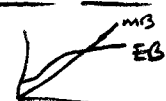
$X_{EB} = f(T)$

grunt work

find H's,  $C_p$ 's

Notice  $\hat{C}_p \neq \tilde{C}_p$  in eqn E8-4.6

$T \quad X_{MB} \quad X_{EB}$



$T = 613\text{R}$  which  $> 585\text{R}$

Can't use

Example 8-8 continued

11/52

V Given  $\Rightarrow$  CSTR adiabatic steady-state

Mole balance

$$0 = F_0 X - k C_p V$$

$$C_p \text{ liquid phase} = \frac{F}{V} = \frac{F_0 (1-X)}{V_0}$$

$$0 = F_{p0} X_p - k \frac{F_{p0}}{V_0} (1-X) V = \boxed{X_p - k \tau (1-X_p) = 0}$$

Solve for X

$$\frac{F_{p0} X_p}{(1-X_p)} = k \frac{F_{p0} V}{V_0} = k \tau \quad \uparrow \quad A \exp(-E_A/RT)$$

$f(X)$

$f(\tau)!$

one equation 2 unknowns

or solving for X

$$X_p = k \tau - k \tau X_p$$

$$X_p + k \tau X_p = k \tau$$

$$\boxed{X_p = \frac{k \tau}{1 + k \tau}}$$

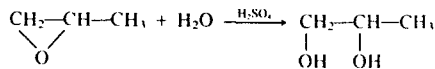
526 4th

However, it is difficult to detect multiple solutions with a numerical procedure.

The algorithm for working through either Case A or B is summarized in Figure 8-3. Its application is illustrated in the following example.

8-8 Example 8-8 Production of Propylene Glycol in an Adiabatic CSTR

Propylene glycol is produced by the hydrolysis of propylene oxide:



Over 800 million pounds of propylene glycol were produced in 1990 and the selling price was approximately \$0.56 per pound. Propylene glycol makes up about 25% of the major derivatives of propylene oxide. The reaction takes place readily at room temperature when catalyzed by sulfuric acid.

You are the engineer in charge of an adiabatic CSTR producing propylene glycol by this method. Unfortunately, the reactor is beginning to leak, and you must replace it. (You told your boss several times that sulfuric acid was corrosive and that mild steel was a poor material for construction.) There is a nice overflow CSTR of 300-gal capacity standing idle; it is glass-lined and you would like to use it.

You are feeding 2500 lb/h (43.03 lb mol/h) of propylene oxide (P.O.) to the reactor. The feedstream consists of (1) an equivolometric mixture of propylene oxide (46.62 ft<sup>3</sup>/h) and methanol (46.62 ft<sup>3</sup>/h), and (2) water containing 0.1 wt% H<sub>2</sub>SO<sub>4</sub>. The volumetric flow rate of water is 233.1 ft<sup>3</sup>/h, which is 2.5 times the methanol-P.O. flow rate. The corresponding molar feed rates of methanol and water are 71.87 and 802.8 lb mol/h, respectively. The water-propylene oxide-methanol mixture undergoes a slight decrease in volume upon mixing (approximately 3%), but you neglect this decrease in your calculations. The temperature of both feedstreams is 58°F prior to mixing, but there is an immediate 17°F temperature rise upon mixing of the two feedstreams caused by the heat of mixing. The entering temperature of all feedstreams is thus taken to be 75°F (see Figure E8-4.1).

Furusawa et al.<sup>6</sup> state that under conditions similar to those at which you are operating, the reaction is first-order in propylene oxide concentration and apparent zero-order in excess of water with the specific reaction rate

$$k = Ae^{-E/RT} = 16.96 \times 10^{12} (e^{-32,400/RT}) \text{ h}^{-1}$$

The units of  $E$  are Btu/lb mol.

There is an important constraint on your operation. Propylene oxide is a rather low-boiling substance (b.p. at 1 atm, 93.7°F). With the mixture you are using, you feel that you cannot exceed an operating temperature of 125°F, or you will lose too much oxide by vaporization through the vent system.

Can you use the idle CSTR as a replacement for the leaking one if it will be operated adiabatically? If so, what will be the conversion of oxide to glycol?

<sup>6</sup> T. Furusawa, H. Nishimura, and T. Miyauchi, *J. Chem. Eng., Jpn.*, 2, 95 (1969).

start this problem  
derive mole balance  
ask the question  
what is the value of T?

$F_{A0} = 43.03 \text{ lbmol/hr}$   
 $Q_A = 46.62 \text{ ft}^3/\text{hr}$   
 $Q_M = 46.62 \text{ ft}^3/\text{hr}$   
0.1% H<sub>2</sub>SO<sub>4</sub> wt

300 gal Reactor

$T_{\text{max}} = 125^\circ\text{F}$

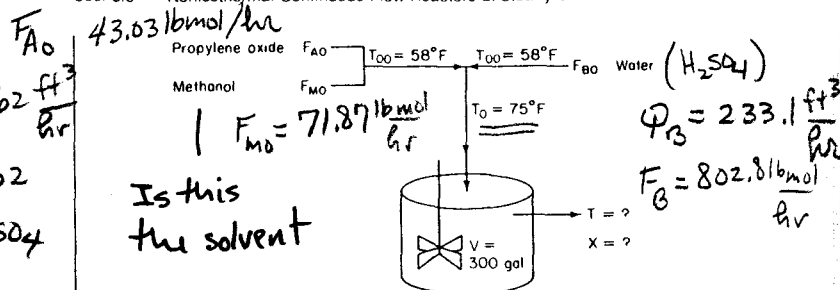
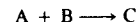


Figure E8-4.1

Solution

(All data used in this problem were obtained from the *Handbook of Chemistry and Physics* unless otherwise noted.) Let the reaction be represented by



in which

- A is propylene oxide (MW = 58.08;  $\rho = 0.859 \text{ g/cm}^3$ ;  $C_p = 35 \text{ Btu/lb mol} \cdot ^\circ\text{F}$ )
- B is water (MW = 18.02;  $\rho = 0.9941 \text{ g/cm}^3$ ;  $C_p = 18 \text{ Btu/lb mol} \cdot ^\circ\text{F}$ )
- C is propylene glycol (MW = 76.11;  $\rho = 1.036 \text{ g/cm}^3$ ;  $C_p = 46 \text{ Btu/lb mol} \cdot ^\circ\text{F}$ )
- M is methanol (MW = 32.04;  $\rho = 0.7914 \text{ g/cm}^3$ ;  $C_p = 19.5 \text{ Btu/lb mol} \cdot ^\circ\text{F}$ )

In this problem neither the exit conversion nor the temperature of the adiabatic reactor is given. By application of the material and energy balances we can solve two equations with two unknowns ( $X$  and  $T$ ). Solving these coupled equations, we determine the exit conversion and temperature for the glass-lined reactor to see if it can be used to replace the present reactor.

1. Mole balance and design equation:

$$F_{A0} - F_A + r_A V = 0$$

The design equation in terms of  $X$  is

$$V = \frac{F_{A0} X}{-r_A} \quad (\text{E8-4.1})$$

2. Rate law:

$$-r_A = k C_A \quad (\text{E8-4.2})$$

<sup>7</sup> Estimated from the observation that the great majority of low-molecular-weight oxygen-containing organic liquids have a mass heat capacity of  $0.6 \text{ cal/g} \cdot ^\circ\text{C} \pm 15\%$ .

\*\*\*

3. Stoichiometry (liquid-phase,  $v = v_0$ ):

$$C_A = C_{A0}(1 - X) \quad (\text{E8-4.3})$$

## 4. Combining yields

$$V = \frac{F_{A0}X}{kC_{A0}(1 - X)} = \frac{v_0X}{k(1 - X)} \quad (\text{E8-4.4})$$

5. Solving for  $X$  as a function of  $T$  and recalling that  $\tau = V/v_0$  gives

$$X = \frac{\tau k}{1 + \tau k} = \frac{\tau A e^{-E/RT}}{1 + \tau A e^{-E/RT}} \quad (\text{E8-4.5})$$

This equation relates temperature and conversion through the mole balance.

## 6. The energy balance for this adiabatic reaction in which there is negligible energy input provided by the stirrer is

$$-X[\Delta H_R^\circ(T_R) + \Delta \hat{C}_p(T - T_R)] = \sum \Theta_i \hat{C}_{pi}(T - T_0) \quad (\text{8-41})$$

Solving for  $X$ , we obtain

$$X = \frac{\sum \Theta_i \hat{C}_{pi}(T - T_0)}{-[\Delta H_R^\circ(T_R) + \Delta \hat{C}_p(T - T_R)]} \quad (\text{E8-4.6})$$

This equation relates  $X$  and  $T$  through the energy balance. We see that there are two equations [equations (E8-4.5) and (E8-4.6)] that must be solved for the two unknowns,  $X$  and  $T$

## 7. Calculations:

a. Heat of reaction at temperature  $T$ :

$$\Delta H_R(T) = \Delta H_R^\circ(T_R) + \Delta \hat{C}_p(T - T_R) \quad (\text{8-27})$$

$$H_A^\circ(68^\circ\text{F}): -66,600 \text{ Btu/lb mol}^\circ$$

$$H_B^\circ(68^\circ\text{F}): -123,000 \text{ Btu/lb mol}$$

$$H_C^\circ(68^\circ\text{F}): -226,000 \text{ Btu/lb mol}^\circ$$

$$\Delta H_R^\circ(68^\circ\text{F}) = -226,000 - (-123,000) - (-66,600)$$

$$= -36,400 \text{ Btu/lb mol propylene oxide}$$

$$\Delta \hat{C}_p = \hat{C}_{pC} - \hat{C}_{pB} - \hat{C}_{pA}$$

$$= 46 - 18 - 35 = -7 \text{ Btu/lb mol}^\circ\text{F}$$

$$\Delta H_R(T) = -36,400 - (7)(T - 528) \quad (\text{E8-4.7})$$

b. Stoichiometry ( $C_{A0}$ ,  $\Theta_i$ ,  $\tau$ ): The volumetric flow rate entering the reactor is

$$v_0 = v_{A0} + v_{M0} + v_{B0} \quad (\text{E8-4.8})$$

$$= 46.62 + 46.62 + 233.1 = 326.3 \text{ ft}^3/\text{h}$$

$$V = 300 \text{ gal} = 40.1 \text{ ft}^3$$

See Perry's  
Section  
3-147

\* Calculated from heat-of-combustion data.

$$\tau = \frac{V}{v_0} = \frac{40.1 \text{ ft}^3}{326.3 \text{ ft}^3/\text{h}} = 0.1229 \text{ h} \quad (\text{E8-4.9})$$

$$C_{A0} = \frac{F_{A0}}{v_0} = \frac{43.04 \text{ lb mol/h}}{326.3 \text{ ft}^3/\text{h}} = 0.132 \text{ lb mol/ft}^3$$

$$\text{For methanol: } \Theta_M = \frac{F_{M0}}{F_{A0}} = \frac{71.87 \text{ lb mol/h}}{43.04 \text{ lb mol/h}} = 1.67$$

For water:

$$\Theta_B = \frac{F_{B0}}{F_{A0}} = \frac{802.8 \text{ lb mol/h}}{43.04 \text{ lb mol/h}} = 18.65$$

## c. Energy balance terms:

$$\begin{aligned} \sum \Theta_i \hat{C}_{pi} &= \hat{C}_{pA} + \Theta_B \hat{C}_{pB} + \Theta_M \hat{C}_{pM} + 0 \hat{C}_{pC} \quad (\text{E8-4.10}) \\ &= 35 + (18.65)(18) + (1.67)(19.5) \\ &= 403.3 \text{ Btu/lb mol}^\circ\text{F} \end{aligned}$$

$$\begin{aligned} T_0 &= T_{00} + \Delta T_{\text{mix}} = 58^\circ\text{F} + 17^\circ\text{F} = 75^\circ\text{F} \quad (\text{E8-4.11}) \\ &= 535^\circ\text{R} \end{aligned}$$

$$T_R = 68^\circ\text{F} = 528^\circ\text{R}$$

The conversion calculated from the energy balance,  $X_{EB}$ , for an adiabatic reaction is found by rearranging Equation (8-41):

$$X_{EB} = - \frac{\sum \Theta_i \hat{C}_{pi}(T - T_0)}{\Delta H_R^\circ(T_R) + \Delta \hat{C}_p(T - T_R)} \quad (\text{E8-4.6})$$

Substituting all the known quantities into the mole and energy balances gives us

$$\begin{aligned} X_{EB} &= \frac{(403.3 \text{ Btu/lb mol}^\circ\text{F})(T - 535)^\circ\text{F}}{-[-36,400 - 7(T - 528)] \text{ Btu/lb mol}} \\ &= \frac{403.3(T - 535)}{36,400 + 7(T - 528)} \quad (\text{E8-4.12}) \end{aligned}$$

The conversion calculated from the mole balance,  $X_{MB}$ , is found from Equation (E8-4.5).

$$\begin{aligned} X_{MB} &= \frac{(16.96 \times 10^{12} \text{ h}^{-1})(0.1229 \text{ h}) \exp(-32,400/1.987T)}{1 + (16.96 \times 10^{12} \text{ h}^{-1})(0.1229 \text{ h}) \exp(-32,400/1.987T)} \\ &= \frac{(2.084 \times 10^{12}) \exp(-16,306/T)}{1 + (2.084 \times 10^{12}) \exp(-16,306/T)} \quad (\text{E8-4.13}) \end{aligned}$$

8. Solving: There are a number of different ways to solve these two simultaneous equations [e.g., substituting Equation (E8-4.12) into (E8-4.13)]. To give insight into the functional relationship between  $X$  and  $T$  for the mole and energy balances, we shall obtain a graphical

Plot  $X_{EB}$  as a function of temperature

Plot  $X_{MB}$  as a function of temperature

TABLE E8-4.1

T (°R)	X <sub>MB</sub> [Eq. (E8-4.13)]	X <sub>EB</sub> [Eq. (E8-4.12)]
535	0.108	0.000
550	0.217	0.166
565	0.379	0.330
575	0.500	0.440
585	0.620	0.550
595	0.723	0.656
605	0.800	0.764
615	0.860	0.872
625	0.900	0.980

solution. Here  $X$  is plotted as a function of  $T$  for the mole and energy balances, and the intersection of the two curves gives the solution where both the mole and energy balance solutions are satisfied. In addition, by plotting these two curves we can learn if there is more than one intersection (i.e., multiple steady states) for which both the energy balance and mole balance are satisfied. If numerical root-finding techniques were used to solve for  $X$  and  $T$ , it would be quite possible to obtain only one root, when there is actually more than one. We shall discuss multiple steady states further in Section 8.7. We choose  $T$  and then calculate  $X$  (Table E8-4.1). The calculations are plotted in Figure E8-4.2. The virtually straight line corresponds to the energy balance [Equation (E8-4.12)] and the curved line corresponds to the mole balance [Equation (E8-4.13)]. We observe from this plot that the only intersection point is at 85% conversion and

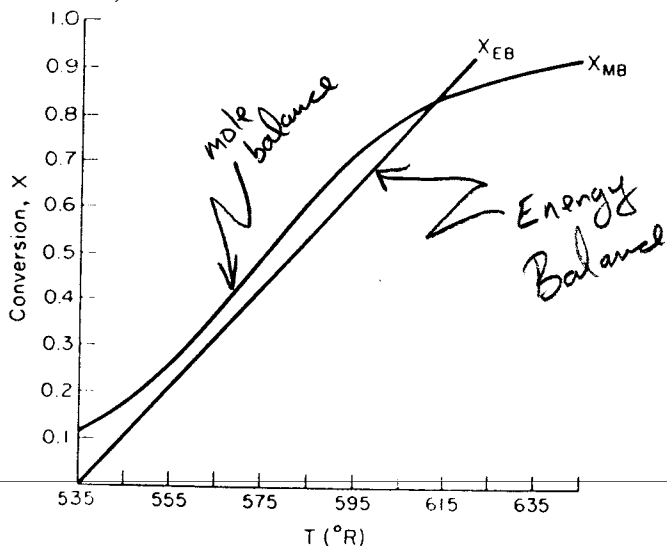


Figure E8-4.2

IN 3rd Edition  
Polymath  
soln  
given

f(x) = X - EB  
f(T) = X - MB  
see p. 450

613°R. At this point both the energy balance and mole balance are satisfied. Because the temperature must remain below 125°F (585°R), we cannot use the 300-gal reactor as it is now.

Example 8-5 CSTR with a Cooling Coil

A cooling coil has been located for use in the hydration of propylene oxide discussed in Example 8-4. The cooling coil has 40 ft<sup>2</sup> of cooling surface and the cooling water flow rate inside the coil is sufficiently large that a constant coolant temperature of 85°F can be maintained. A typical overall heat-transfer coefficient for such a coil is 100 Btu/h-ft<sup>2</sup>-°F. Will the reactor satisfy the previous constraint of 125°F maximum temperature if the cooling coil is used?

Solution

If we assume that the cooling coil takes up negligible reactor volume, the conversion calculated as a function of temperature from the mole balance is the same as that in Example 8-4 [Equation (E8-4.13)].

1. Combining the mole balance, stoichiometry, and rate law, we have

is before 
$$X_{MB} = \frac{2.084 \times 10^{12} \exp(-16,306/T)}{1 + 2.084 \times 10^{12} \exp(-16,306/T)} \quad (E8-4.13)$$

2. Energy balance: Neglecting the work done by the stirrer, we combine equations (8-34) and (8-40) to obtain

$$\frac{UA(T_a - T)}{F_{A0}} - X[\Delta H_R^0(T_R) + \Delta \hat{C}_p(T - T_R)] = \sum \theta_i \hat{C}_{pi}(T - T_0) \quad (E8-5.1)$$

New term

Solving the energy balance for  $X_{EB}$  yields

$$X_{EB} = \frac{\sum \theta_i \hat{C}_{pi}(T - T_0) + [UA(T - T_a)/F_{A0}]}{-[\Delta H_R^0(T_R) + \Delta \hat{C}_p(T - T_R)]} \quad (E8-5.2)$$

The cooling coil term in Equation (E8-5.2) is

$$\frac{UA}{F_{A0}} = 100 \frac{\text{Btu}}{\text{h-ft}^2\text{-}^\circ\text{F}} \left( \frac{40 \text{ ft}^2}{43.04 \text{ lb mol/h}} \right) = \frac{92.9 \text{ Btu}}{\text{lb mol-}^\circ\text{F}} \quad (E8-5.3)$$

Recall that the cooling temperature is

$$T_a = 85^\circ\text{F} = 545^\circ\text{R}$$

The numerical values of all other terms of Equation (E8-5.2) are identical to those given in Equation (E8-4.12):

$$X_{EB} = \frac{403.3(T - 535) + 92.9(T - 545)}{36,400 + 7(T - 528)} \quad (E8-5.4)$$

From Table E8-5.1 we see that at a temperature of 564°R, both the mole balance and energy balance are satisfied and the corresponding conversion is

TABLE E8-5.1

$T$	$X_{MB}$ [Eq. (E8-4.13)]	$X_{EB}$ [Eq. (E8-5.4)]
535	0.108	-0.025
550	0.217	0.178
→ 564	0.367	0.367
565	0.379	0.381
570	0.440	0.448
575	0.500	0.515
585	0.620	0.649
595	0.723	0.784

37%. Consequently, we can use the 300-gal reactor with the cooling coil successfully at a reactor temperature of 104°F. A plot of equations (E8-4.13) and (E8-5.4) will verify that there is only one steady state, at  $X = 0.37$  and  $T = 104^\circ\text{F}$  ( $564^\circ\text{R}$ ).

### 8.3.2 Adiabatic Tubular Reactor

*(see later)*

The energy balance given by Equation (8-38) relates the conversion at any point in the reactor to the temperature of the reaction mixture at the same point (i.e., it gives  $X$  as a function of  $T$ ). Usually, there is a negligible amount of work done on or by the reacting mixture, so normally, the work term can be neglected in tubular reactor design. However, unless the reaction is carried out adiabatically, Equation (8-38) is still difficult to evaluate, because in nonadiabatic reactors, the heat added to or removed from the system varies along the length of the reactor. This problem does not occur in adiabatic reactors, which are frequently found in industry. Therefore, the adiabatic tubular reactor will be analyzed first.

Because  $\dot{Q}$  and  $W_s$  are equal to zero for the reasons stated above, Equation (8-38) reduces to

$$X[-\Delta H_R(T)] = \int_{T_0}^T \sum \theta_i C_{pi} dT \quad (8-43)$$

This equation can be combined with the differential mole balance

$$F_{A0} \frac{dX}{dV} = -r_A(X, T)$$

to obtain the temperature, conversion, and concentration profiles along the length of the reactor. One way of accomplishing this combination is to use Equation (8-43) to construct a table of  $T$  as a function of  $X$ . Once we have  $T$  as a function of  $X$ , we can obtain  $k(T)$  as a function of  $X$  and hence  $-r_A$  as a function of  $X$  alone. We then use the procedures detailed in Chapter 2 to size the different types of reactors.

Consider the elementary reversible gas-phase reaction



carried out in a PFR in which pressure drop is neglected and pure A enters the reactor.

Design equation:

$$V = F_{A0} \int_0^X \frac{dX}{-r_A}$$

Rate law:

$$-r_A = k \left( C_A - \frac{C_B}{K_c} \right)$$

Stoichiometry ( $\epsilon = 0.0$ ):

$$C_A = C_{A0}(1 - X) \frac{T_0}{T}$$

$$C_B = C_{A0}X \frac{T_0}{T}$$

Combining the design equation, rate law, and stoichiometry, we have

$$V = F_{A0} \int_0^X \frac{dX}{k C_{A0} [(1 - X) - (X/K_c)] (T_0/T)}$$

To determine the energy balance, we now solve Equation (8-43) for  $T$  as a function of  $X$  and then use the equations to calculate  $k(T)$  and  $K_c(T)$  at a given value of  $X$ . One procedure to evaluate this integral is to

1. Choose  $X = 0$ .
2. Calculate  $T$  from the energy balance Equation (8-43):

$$X = \frac{\int_{T_0}^T \sum \theta_i C_{pi} dT}{-\Delta H_R(T)}$$

For example, integrating Equation (8-43), using the mean heat capacities, and assuming  $T_0 = T_0$ , we have

$$X = \frac{\sum \theta_i \hat{C}_{pi} (T - T_0)}{-[\Delta H_R^\circ(T_R) + \Delta \hat{C}_p (T - T_R)]}$$

Solving for  $T$  yields

$$T = \frac{X[-\Delta H_R^\circ(T_R)] + \sum \theta_i \hat{C}_{pi} T_0 + X \Delta \hat{C}_p T_R}{\sum \theta_i \hat{C}_{pi} + X \Delta \hat{C}_p}$$

3. Calculate  $T/T_0$ .

This is an algorithm for an adiabatic PFR

*Polymath on page*

Example 8-8 Adiabatic CSTR

POLYMATH Report

Nonlinear Equations

Calculated values of NLE variables

Variable	Value	f(x)	Initial Guess
1 T	613.658	3.334E-09	600.
2 X	0.8573814	7.478E-11	0.8

Variable	Value
1 A	1.696E+13
2 E	3.24E+04
3 k	48.91545
4 R	1.987
5 tau	0.1229

Nonlinear equations

1  $f(X) = X - (403.3 * (T - 535)) / (36400 + 7 * (T - 528)) = 0$

2  $f(T) = X - \tau * k / (1 + \tau * k) = 0$

Explicit equations

1  $\tau = 0.1229$

2  $A = 16.96 * 10^{12}$

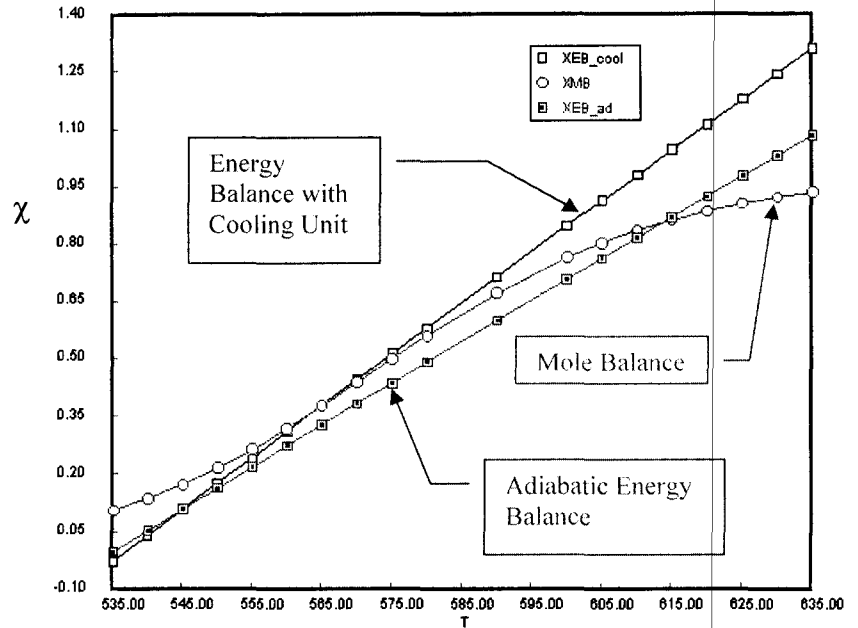
3  $E = 32400$

4  $R = 1.987$

5  $k = A * \exp(-E / (R * T))$

Example 8-8 Propylene Glycol Production - Adiabatic CSTR

19-Mar-2007



Example 8-8 CSTR with Cooling Coil  $\frac{UA}{F_{A0}} = 92.9 \frac{\text{Btu}}{\text{lbmol}^\circ\text{F}}$   $T_a = 545 \text{ R}$

Calculated values of NLE variables

Variable	Value	f(x)	Initial Guess
1 T	563.7289	-5.411E-10	564.
2 X	0.3636087	2.243E-11	0.367

Variable	Value
1 A	1.696E+13
2 E	3.24E+04
3 k	4.648984
4 R	1.987
5 tau	0.1229

Nonlinear equations

1  $f(X) = X - (403.3 * (T - 535) + 92.9 * (T - 545)) / (36400 + 7 * (T - 528)) = 0$

2  $f(T) = X - \tau * k / (1 + \tau * k) = 0$

Explicit equations

1  $\tau = 0.1229$

2  $A = 16.96 * 10^{12}$

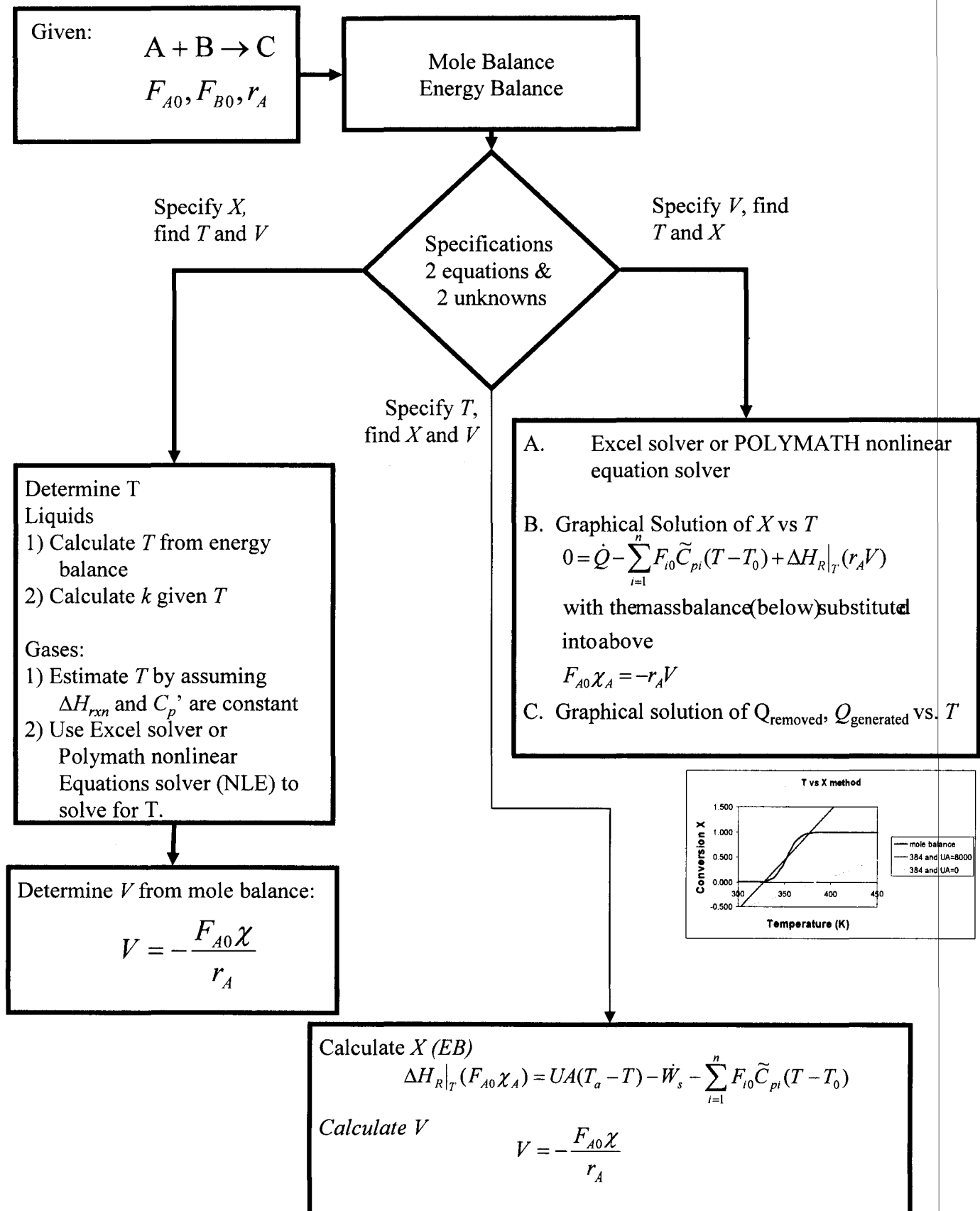
3  $E = 32400$

4  $R = 1.987$

5  $k = A * \exp(-E / (R * T))$

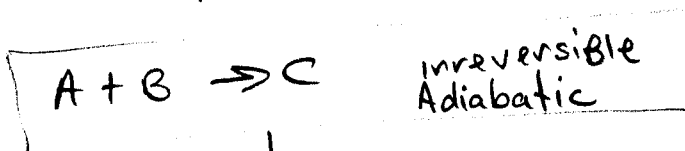


## Energy Balance Algorithm for CSTR Design – Figure 8-13, p525&amp;526 revised



# p 443 - modified

Ad



mole Balances  
Heat Balance

$r_A = -k C_A^m C_B^n$   
 $k = A \exp(-E_a/RT)$   
 $C_A = F_A/Q$  ← for gases there is a T dependence!

$X_A$  GIVEN

V GIVEN

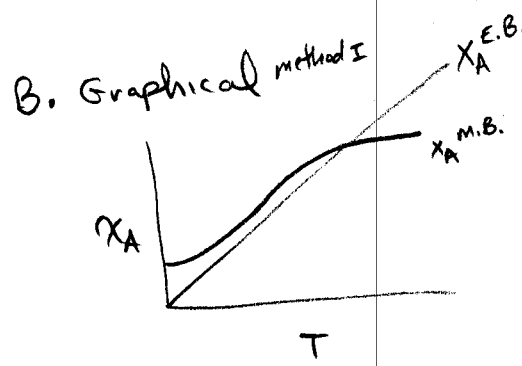
Specifications

find  $V \neq T$

find  $X_A \neq T$

USE Heat balance to find T

A. Analytical  
2 eqns 2 unknowns



Note: liquids - explicit solution - see text p. 399  
gases - Trial & error

- ① Analytical → Step 1 Rough Guess of T  
assume  $\Delta H_{rxn} = \text{constant}$  &  $c_p$  are constant
- ② Graphical: plot  $\phi$  vs T  
 ← flow  
 ← rxn  
 ← line  
 ← curve  
Step 2 Use Root finder for Polymath (or Newton Raphson etc.) solve for T given initial guess

$V = -\frac{F_{A0} X_A}{r_A}$  ← function of T

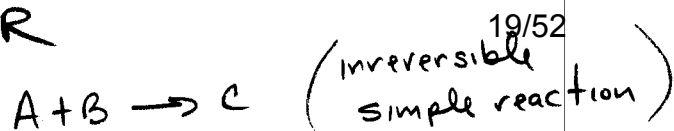
M.B.  $0 = F_{A0} X_A + r_A(X_A, T) V$

again →

E.B.  $X_A = \frac{\sum F_{i0} \hat{c}_{p,i} (T - T_{i0}) - \dot{Q}}{-\Delta H_{rxn} F_{A0}}$

T specify →  
 $X_A^{M.B.}$  calculate →  
 $X_A^{E.B.}$

## 8.3.1 steady-state CSTR



$$\frac{dT}{dt} = 0$$

Mole Balances:

$$0 = F_{A0} - F_A + r_A V$$

$$0 = F_{B0} - F_B + \frac{b}{a} r_A V$$

$$0 = F_{C0} - F_C - \frac{c}{a} r_A V$$

$$X_A = \frac{F_{A0} - F_A}{F_{A0}}$$

$$0 = F_{A0} X_A + r_A V$$

Heat balance:

$$0 = \dot{Q} - \dot{W}_s - \sum_{i=1}^N F_{i0} \tilde{C}_{P_i} (T - T_{i0}) - \Delta H_{rxn} (-r_A V)$$

CASE 0 - Isothermal - no heat balance!

CASE I Adiabatic  $\dot{Q} = 0$   $\dot{W}_s = 0$

CASE II NON-adiabatic

CASE I  $\dot{Q} = 0$   $\dot{W}_s = 0$

① from mole balance:  $r_A V = -(F_{A0} - F_A) = -F_{A0} X_A$   
 these two can be related

②  $\sum F_{i0} \tilde{C}_{P_i} (T - T_{i0}) = -\Delta H_{rxn} F_{A0} X_A$   
 $\frac{(\text{mol l}^{-1} \text{ in}) \text{ kJ}}{\text{s mol l}^{-1} \text{ K}} \text{ K} = \frac{\text{kJ}}{\text{mol A React}} \frac{(\text{mol A in})}{\text{s}} \frac{\text{mol A React}}{\text{mol A in}}$

This is a straight line for EB

unknowns:  $T, X_A$

AND:  $\Delta H_{rxn} = f(T \text{ and } X_A)$

$r_A = f(T \text{ \& } X_A)$

# CASE II Nonadiabatic : Graphical methods

$X_A$  vs  $T$   
20/52

Mole Balance:  $0 = F_{A0} - F_A + r_A V = X_A F_{A0} + r_A V$  (1)

Energy Balance:  $0 = -\sum F_{i0} \sum C_{p,i} (T - T_0) + \Delta H_{rxn} r_A V + \dot{Q} - \dot{W}_s$

Assume  $\dot{W}_s = 0$   
 $\dot{Q} = UA(T_a - T)$  (Heat added to C.V. is positive if  $T_a > T$ , is negative if  $T_a < T$ )

(2)  $\sum F_{i0} C_{p,i} (T - T_0) - UA(T_a - T) = \Delta H_{rxn} r_A V$

Two equations: <sup>MB</sup> 1  $\neq$  <sup>EB</sup> 2

unknowns:  $V, X_A \neq T$  } Need to specify 1 variable if  $V$  is specified:

Solve M.B. for  $X_A$  if possible (see p 399 for 1<sup>st</sup> order kinetics)

Use ~~2-3 Back solver~~ Excel Solver

$0 = X_A F_{A0} + r_A V$

Procedure: Specify  $T$  calculate  $X_A$   
 excel spreadsheet

<u>T</u>	<u><math>X_A</math></u>	<u><math>f(X_A \neq T)</math></u>
100	guess1	make = 0
110		
120		
130		

$k = A \exp\left(-\frac{E}{RT}\right)$

$r_A$  is very sensitive to  $T$   
 $0 < X_A \leq X_{eq} \leq 1$

iterate on this cell to make this cell zero

E.B. substitute  $F_{A0} X_A$  for  $-r_A V$   
from M.B.

$$\sum F_{i0} C_{p_i} (T - T_0) - UA(T_a - T) = -\Delta H_{rxn} F_{A0} X_A$$

↑  
only place  
in which  $X_A$   
appears

$$X_A = \frac{\sum F_{i0} C_{p_i} (T - T_0) - UA(T_a - T)}{-\Delta H_{rxn} F_{A0}}$$

A straight  
line

$$= T \left[ \underbrace{\frac{(\sum F_{i0} C_{p_i} + UA)}{-\Delta H_{rxn} F_{A0}}}_{\text{slope} = S} \right] + \underbrace{\left[ \frac{-\sum F_{i0} C_{p_i} T_0 - UA T_a}{-\Delta H_{rxn} F_{A0}} \right]}_I$$

different  $T$ 's

$S > 0$   $\Delta H_{rxn} < 0$  exothermic  
 $S < 0$   $\Delta H_{rxn} > 0$  endothermic

I: varies

spread sheet continued

T	$X_A$ M.B.	$f(X_A, T)$	$\Delta H_{rxn}$	Cp's			$X_A$ E.B. from T in column 1
	guess	make = 0		A	B	C	
100			/	/	/	/	
110			/	/	/	/	
120			/	/	/	/	
130			/	/	/	/	

straight  
calculation

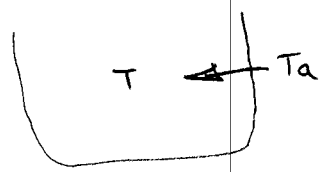
CASE II Non-adiabatic : Graphical Methods 22/52  $\Phi_R = \Phi_G$

Mole balance:  $0 = F_{A0} - F_A + r_A V = X_A F_{A0} + r_A V$

Energy balance  $0 = -\sum F_{i0} C_{p_i} (T - T_0) + (\Delta H_{rxn}) r_A V + \dot{Q} - \dot{W}_s$   
 $\dot{W}_s$  is it negligible? yes

$$\underbrace{\sum F_{i0} C_{p_i} (T - T_0) - \dot{Q}}_{\substack{\text{"Heat Removal" or} \\ \text{"added"}}} = \underbrace{(\Delta H_{rxn}) r_A V}_{\substack{\text{"Heat generated" or} \\ \text{"Heat required"}}$$

exo → endo



if  $\dot{Q} = UA_{HT} (T_a - T)$   
 (positive is adding heat to the system)

if  $T_a > T$  heat is added  
 if  $T_a < T$  heat is removed

Looking at the  $\Phi_{Removed}$  term

$$\Phi_R = \sum F_{i0} C_{p_i} (T - T_0) - UA(T_a - T)$$

$$= \underbrace{(\sum F_{i0} C_{p_i} + UA)}_{\text{slope}} T - \underbrace{\sum F_{i0} C_{p_i} T_0 - UA T_a}_{\text{intercept}}$$

This analysis is useful for stability

504  
8-5

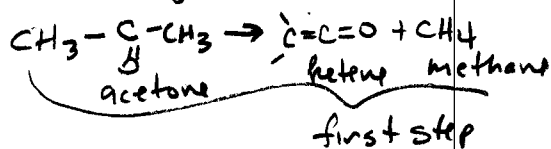
# ENERGY Balance PFR

23/52

Table E8-7.1

Example 8-7

Production of Acetic Anhydride



$$\frac{dF_A}{dV} = r_A \quad \frac{dF_B}{dV} = -r_A \quad F_C = F_B$$

$$r_A = -kC_A$$

$$k = \exp\left[34.34 - \frac{34,222 \text{ K}}{T}\right]$$

$$F_T = F_A + F_B + F_C$$

$$\frac{dT}{dV} = \frac{U_a(T_a - T) + r_A \Delta H_{rxn}}{F_A C_{pA} + F_B C_{pB} + F_C C_{pC}}$$

my equation 13  
in PFR and  
Foglers eqn 8-60

$$\Delta H_{rxn}|_{T_R} = 80,770 \text{ J/mol} \quad \leftarrow \text{watch units}$$

$$C_A = \frac{F_A}{Q}$$

$$Q = \frac{Q_0 P_0 F_T T}{P F_{T_0} T_0} \quad \text{assuming } P = P_0$$

$$\left. \begin{matrix} C_{pA} \\ C_{pB} \\ C_{pC} \end{matrix} \right\} \text{Ideal Gas heat capacities} \quad a + bT + cT^3 \left[ \frac{\text{J}}{\text{mol K}} \right]$$

$$\Delta H_{rxn}|_T = \Delta H_{rxn}|_{T_R} + \Delta C_p (T - T_R)$$

$$\Delta \hat{C}_p = C_{pC} + C_{pB} - C_{pA}$$

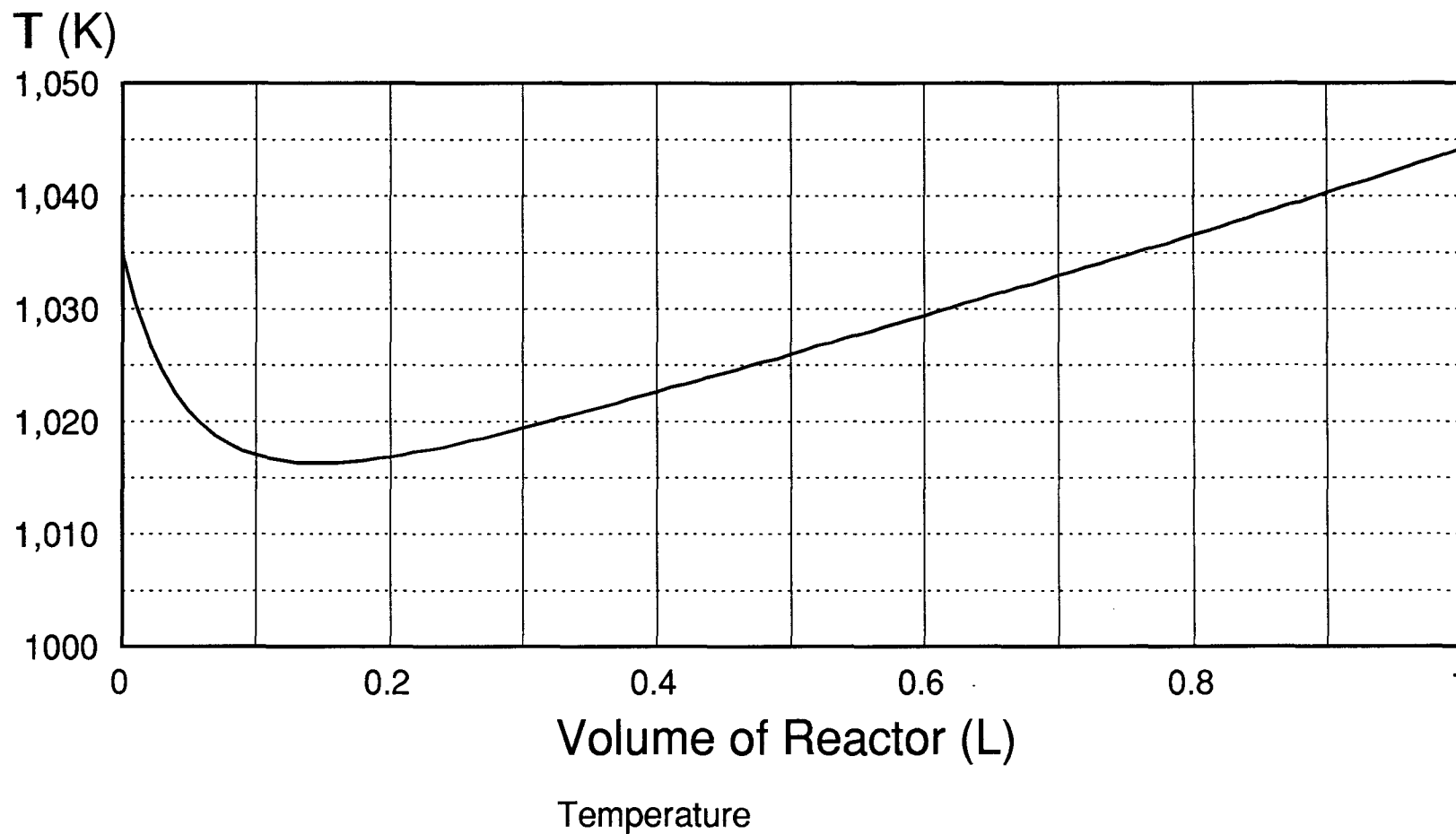
22-141 50 SHEETS  
22-142 100 SHEETS  
22-144 200 SHEETS



# Concentration and Temperature Profiles

Heated Plug Flow Reactor with Endothermic Rxn

Example Problem 8-7 (Fogler 1991)



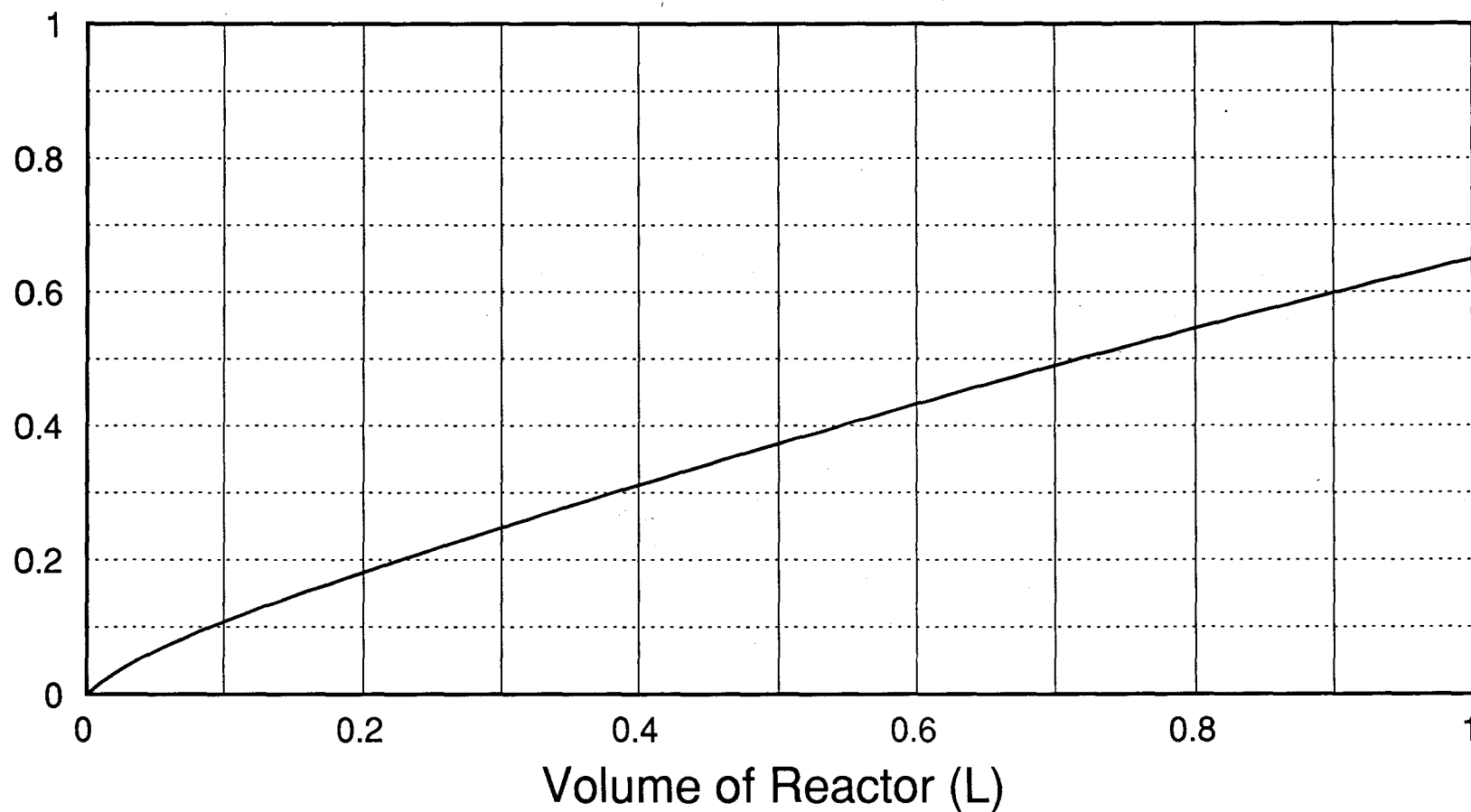


# Concentration and Temperature Profiles

Heated Plug Flow Reactor with Endothermic Rxn

Example Problem 8-7 (Fogler 1991)

Conversion



**POLYMATH 5.0 Results****Example 8-7** 03-22-2000**Calculated values of the DEQ variables**

Variable	initial value	minimal value	maximal value	final value
V	0	0	5	5
X	0	0	0.2684425	0.2684425
T	1035	902.59769	1035	902.59769
Fao	38.3	38.3	38.3	38.3
Cpa	166.90862	154.44403	166.90862	154.44403
delCp	-9.1838673	-9.1838673	-6.6838142	-6.6838142
k	3.5808176	0.0280243	3.5808176	0.0280243
Cao	18.8	18.8	18.8	18.8
To	1035	1035	1035	1035
Tr	298	298	298	298
deltaH	7.876E+04	7.876E+04	7.981E+04	7.981E+04
ra	-67.319371	-67.319371	-0.3484305	-0.3484305

**ODE Report (RK45)**

Differential equations as entered by the user

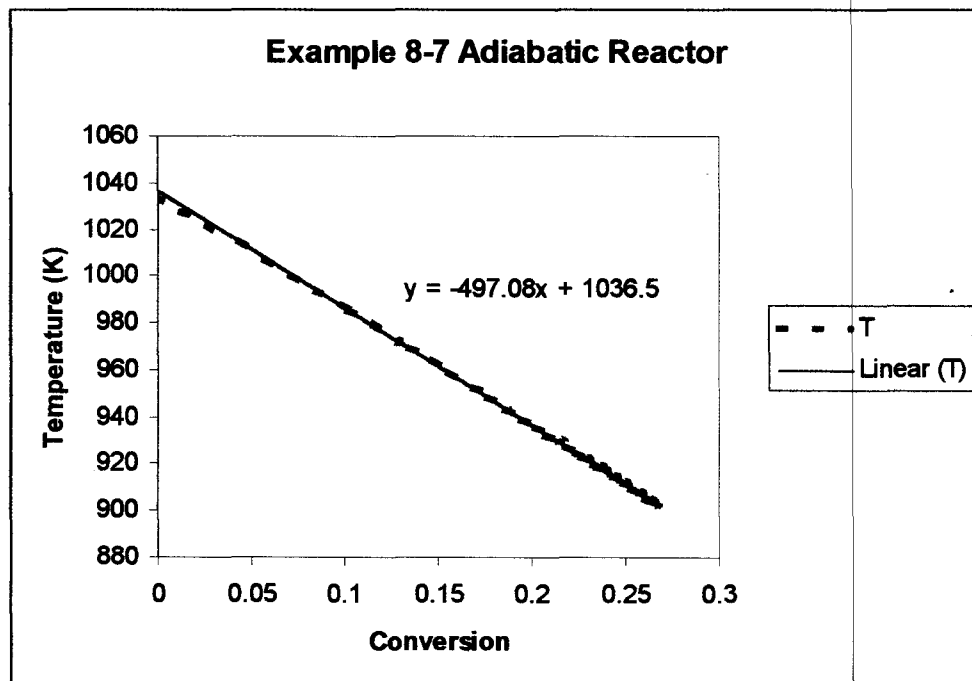
- [1]  $d(X)/d(V) = -ra/Fao$   
 [2]  $d(T)/d(V) = -ra*(-deltaH)/(Fao*Cpa+X*delCp)$

Explicit equations as entered by the user

- [1]  $Fao = 38.3$   
 [2]  $Cpa = 26.63 + .183*T - 45.86*10^{(-6)}*T^2$   
 [3]  $delCp = 6.8 - 11.5*10^{(-3)}*T - 3.81*10^{(-6)}*T^2$   
 [4]  $k = 8.2*10^{14} * \exp(-34222/T)$   
 [5]  $Cao = 18.8$   
 [6]  $To = 1035$   
 [7]  $Tr = 298$   
 [8]  $deltaH = 80770 + 6.8*(T-Tr) - 5.75*10^{(-3)}*(T^2-Tr^2) - 1.27*10^{(-6)}*(T^3-Tr^3)$   
 [9]  $ra = -k*Cao*(1-X)/(1+X)*To/T$

Independent variable

variable name : V  
 initial value : 0  
 final value : 5



**POLYMATH 5.0 Results****Example 8-7 Part B** 03-22-2000**Calculated values of the DEQ variables**

Variable	initial value	minimal value	maximal value	final value
v	0	0	0.001	0.001
x	0	0	0.6590103	0.6590103
t	1035	1016.253	1045.0786	1045.0786
fa0	0.0376	0.0376	0.0376	0.0376
ua	1.65E+04	1.65E+04	1.65E+04	1.65E+04
ta	1150	1150	1150	1150
cpa	166.83577	165.17143	167.7179	167.7179
dcp	-9.1838673	-9.3796454	-8.8220385	-9.3796454
ca0	18.8	18.8	18.8	18.8
t0	1035	1035	1035	1035
term	-1374.4629	-1415.9993	-1299.3832	-1415.9993
dh	7.876E+04	7.866E+04	7.893E+04	7.866E+04
ra	-67.304	-67.304	-18.845559	-18.845559

**ODE Report (RKF45)**

Differential equations as entered by the user

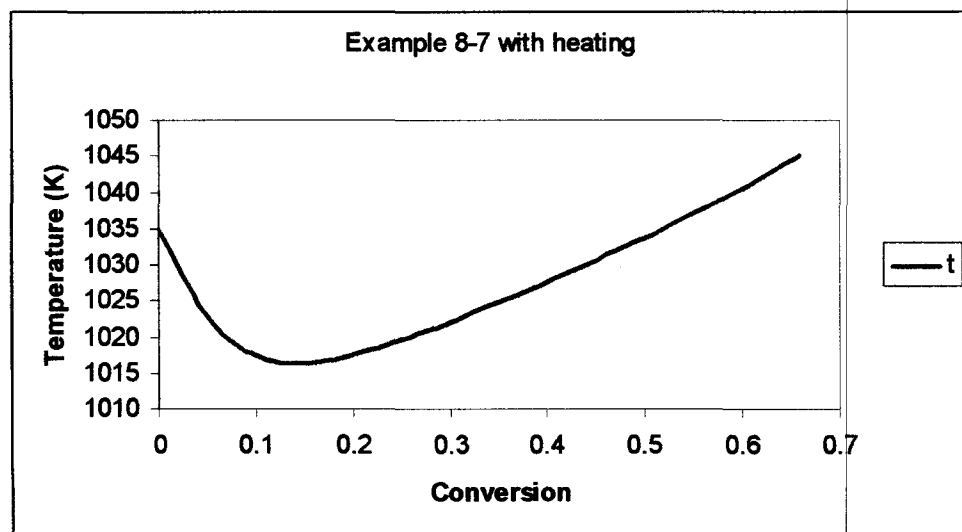
- [1]  $d(x)/d(v) = -ra/fa0$   
 [2]  $d(t)/d(v) = (ua*(ta-t)+ra*dh)/(fa0*(cpa+x*dcp))$

Explicit equations as entered by the user

- [1]  $fa0 = .0376$   
 [2]  $ua = 16500$   
 [3]  $ta = 1150$   
 [4]  $cpa = 26.6 + .183*t - .0000459*t^2$   
 [5]  $dcp = 6.8 - .0115*t - .00000381*t^2$   
 [6]  $ca0 = 18.8$   
 [7]  $t0 = 1035$   
 [8]  $term = -.00000127*(t^3 - 298^3)$   
 [9]  $dh = 80770 + 6.8*(t - 298) - .00575*(t^2 - 298^2) + term$   
 [10]  $ra = -ca0*3.58*exp(34222*(1/t0 - 1/t))*(1-x)*(t0/t)/(1+x)$

Independent variable

variable name : v  
 initial value : 0  
 final value : 0.001



## Notes on Plug Flow Reactors

See page 477 Table 8-1  
-478A) Ideal Exam problem  
Adiabatic  $\dot{q} = 0$   
pure feed  $\rightarrow$ 

$$\sum F_{i0} C_{pi} = F_{A0} C_{PA}$$

$$\Delta H_{rxn} \approx \text{constant}$$

$$\therefore \Delta \hat{C}_p \approx 0$$

$$\Delta C_p \approx 0$$

$$\frac{dT}{dV} = \frac{\Delta H_{rxn} |_{T} r_A}{\sum F_{A0} C_{PA}}$$

B) Hand calculations to check Polymath or Aspen

① assume:  $\Delta H_{rxn} = \text{constant}$  or use an average value

②  $r_A |_{\max} = k C_{A0}$   
↑ feed temperature

③  $C_p = \text{constant}$  (this will vary with T)

$$\frac{\Delta T}{\Delta V} = \frac{\Delta H_{rxn} (-k C_{A0})}{\sum F_{i0} C_{pi}} \quad \text{— put in numbers}$$

C) Units

$$\frac{dT}{dV} = \frac{\Delta H_{rxn} |_{T} r_A + \dot{q}}{\sum F_{i0} C_{pi}}$$

$$\frac{dT}{dW} = \frac{\Delta H_{rxn} r_A + \dot{q}}{\sum F_{i0} C_{pi}}$$

if  $\dot{q} = Ua(T_a - T)$

a must have a change in units  
 $\dot{q}$  — must be  $\frac{J}{s \text{ kg cat}}$   
a = ?

$$U [=] \frac{J}{s \text{ m}^2 \text{ K}}$$

$$T [=] \text{K}$$

$$a [=] \frac{\text{m}^2_{sa}}{\text{m}^3_{\text{Reactor}}}$$

$$\dot{q} [=] \frac{J}{s \text{ m}^2 \text{ K}} \frac{\text{m}^2_{sa}}{\text{m}^3_R} \text{K} = \frac{J}{s \text{ m}^3_R}$$

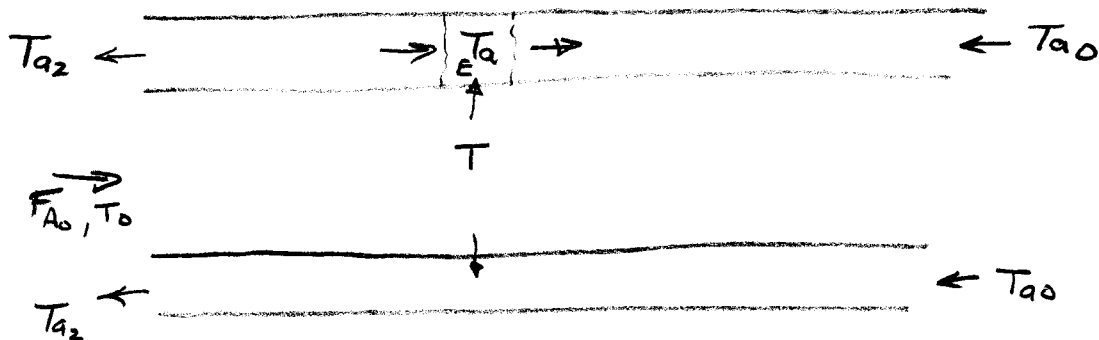
$$\frac{J}{s \text{ m}^2_{sa} \text{ K}} \cdot \frac{\text{m}^2_{sa}}{\text{m}^3_R} \cdot \frac{\text{m}^3_{\text{cat}}}{\text{m}^3_{\text{cat}}} \cdot \frac{\text{m}^3_{\text{cat}}}{\text{kg}_{\text{cat}}} \text{K} \cdot \frac{1}{(1-\phi)} \cdot \frac{1}{\epsilon_c} (T_a - T) = \dot{q}$$

## Section 8.4.2

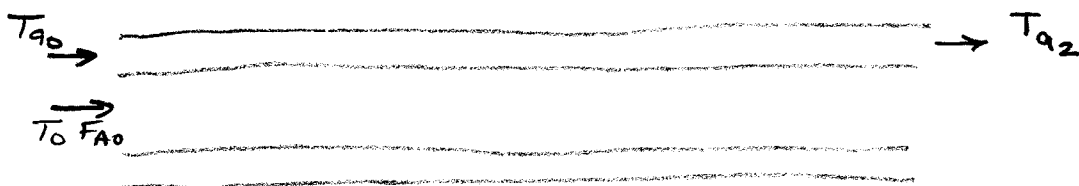
## Co-current vs Counter Current

Energy balance on cooling or heat exchanger fluid

Counter current



Co-current



Energy balance on cooling fluid (Co-current)

$$\frac{\frac{V_{\text{exchanger}}}{V_{\text{react}}} \frac{\partial E}{\partial t}}{0} = \dot{m}_c c_p T_a|_V - \dot{m}_c c_p T_a|_{V+\Delta V} + U_a \Delta V (T - T_a)$$

$$\frac{\text{kg}}{\text{s}} \frac{\text{J}}{\text{kg} \cdot \text{C}} \cdot \text{C} = \frac{\text{J}}{\text{m}^2 \cdot \text{s}} \frac{\text{m}^2}{\text{m}^3} \cdot \text{C}$$

$$\lim_{\Delta V \rightarrow 0} \frac{V_{\text{exch}}}{V_{\text{react}}} \frac{\partial E}{\partial t} = -\dot{m}_c \frac{\partial (c_p T_a)}{\partial V} + U_a (T - T_a)$$

at S.S.

$$\dot{m}_c \frac{\partial (c_p T_a)}{\partial V} = U_a (T - T_a)$$

Co-current  
8-40

$$\dot{m}_c \frac{\partial (c_p T_a)}{\partial V} = -U_a (T - T_a)$$

Counter current  
8-41

# Plug flow Reactors

$$\frac{dT}{dV} = \frac{\Delta H_{rxn}|_T r_A + \dot{q}}{\sum F_{i0} C_{p_i} + \Delta C_p F_{A0} X_A}$$

① If  $\Delta C_p \rightarrow$  small  
or  
 $X_A \rightarrow$  small

then  $\Delta H_{rxn} \sim$  constant  
mole balance  
 $-F_{A0} \frac{dX_A}{dV} = r_A$

②  $\dot{q} = 0$

$$\frac{dT}{dV} = \frac{\Delta H_{rxn}}{\sum F_{i0} C_{p_i}} r_A = \frac{\Delta H_{rxn}}{\sum F_{i0} C_{p_i}} \left( \frac{dF_A}{dV} \right) = \frac{\Delta H_{rxn}}{\sum F_{i0} C_{p_i}} (F_{A0}) \left( -\frac{dX_A}{dV} \right)$$

$$\int_{T_0}^T dT = - \frac{\Delta H_{rxn} F_{A0}}{\sum F_{i0} C_{p_i}} \int_0^{X_A} dX_A$$

$$\frac{\sum F_{i0} C_{p_i} (T - T_0)}{-\Delta H_{rxn} F_{A0}} = X_A \quad \leftarrow \text{for PFR}$$

$$X_A = \frac{\sum (F_{i0}/F_{A0}) C_{p_i} (T - T_0)}{-\Delta H_{rxn}|_T} \quad \leftarrow \text{CSTR}$$

These are the same!

Ⓜ<sub>i</sub> in Book!

# Predicting Equilibrium Constants

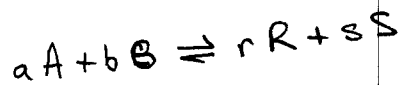
31/52

K<sub>p</sub>-1

see appendix C

P 878<sup>2nd</sup>  
929<sup>3rd</sup>  
1021<sup>4th</sup>

$$K_a \equiv \exp\left(-\frac{\Delta G_{rxn}^\circ}{RT}\right)$$



$$K_a = \prod_{i=1} a_i^{\nu_i} = \frac{a_R^r a_S^s}{a_A^a a_B^b}$$

$\nu_i$  - (stoichiometric coefficient)  
-a, -b, r and s

for an ideal gas

$$a_i = y_i P \text{ or } P_i$$

$$\left\{ \begin{aligned} a_i &\equiv \frac{f_i}{f_i^\circ} = y_i y_i P \\ &= y_i x_i P^{vap} \\ &\text{liquid} \end{aligned} \right.$$

$$\therefore K_a = K_p = \frac{P_R^r P_S^s}{P_A^a P_B^b} = \exp\left(-\frac{\Delta G_{rxn}^\circ}{RT}\right)$$

The equilibrium constant  $K_c$

$$K_c \equiv \frac{C_R^r C_S^s}{C_A^a C_B^b}$$

Converting to pressure  $C_i = \frac{N_i}{V} = \frac{P_i}{RT}$

$$K_c = \frac{(P_R/RT)^r (P_S/RT)^s}{(P_A/RT)^a (P_B/RT)^b} = \frac{P_R^r P_S^s}{P_A^a P_B^b} \left(\frac{1}{RT}\right)^{r+s-a-b}$$

$$\therefore K_c = K_p \left(\frac{1}{RT}\right)^{r+s-a-b}$$

From Figure EC-1.1 we read at 1000 K that  $\log K_p = 0.15$ ; therefore,  $K_p = 1.41$ , which is close to the calculated value. We note that there is no net change in the number of moles for this reaction; therefore,

$$K = K_p = K_c \text{ (dimensionless)}$$

Taking the square root of Equation (EC-1.7) yields

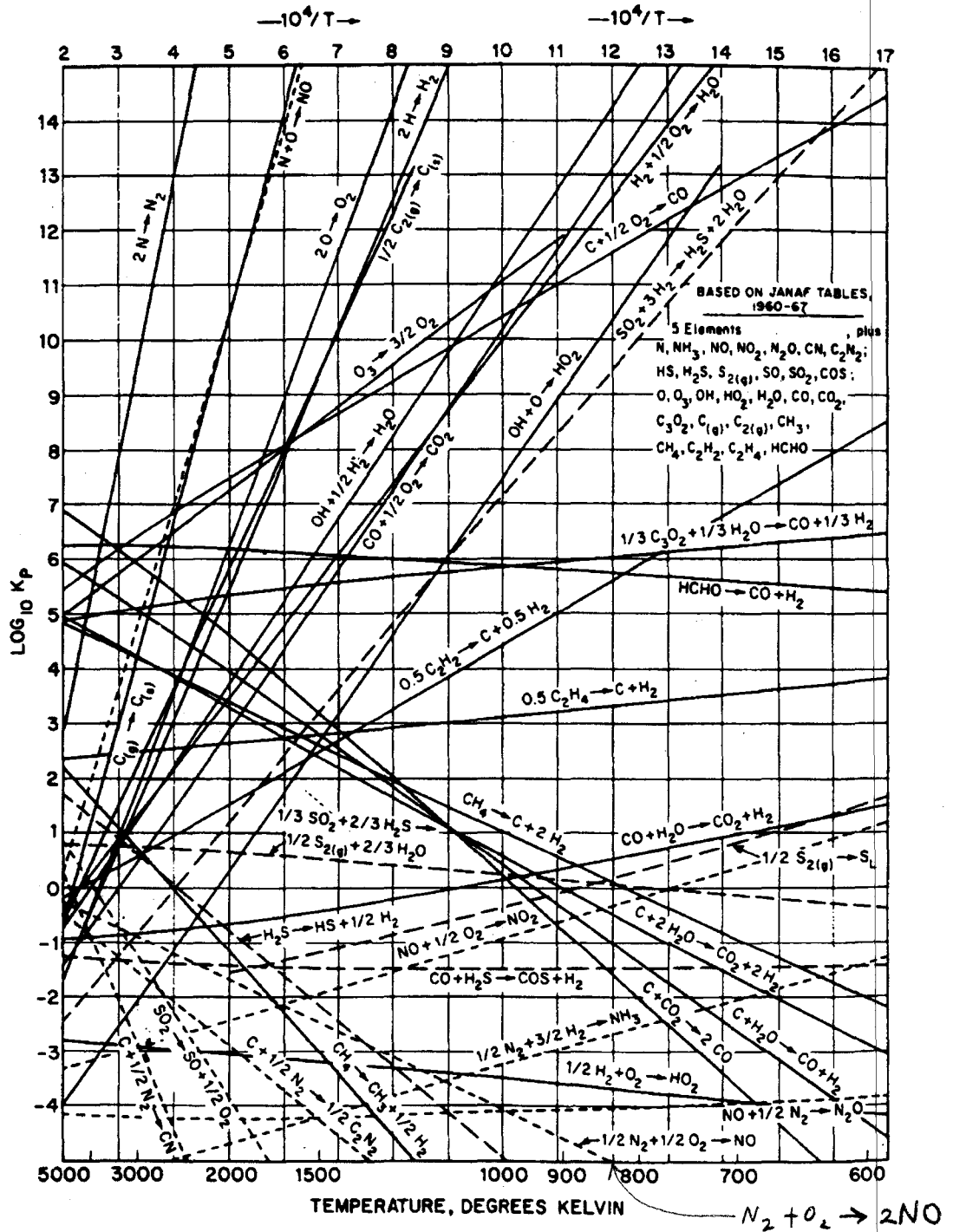


Figure EC-1.1 From M. Modell and R. Reid, *Thermodynamics and Its Applications*, © 1983. Reprinted by permission of Prentice Hall, Inc., Upper Saddle River, N.J.



The van't Hoff equation can be used to adjust the equilibrium constant for temperature

$$\frac{d \ln K_p}{dT} = \frac{\Delta H_{rxn}}{RT^2}$$

↙ a function of T

If  $\Delta H_{rxn}$  is assumed to be constant over small ranges of temperature

$$\ln K_p \Big|_{K_{p1}}^{K_{p2}} = - \left( \frac{\Delta H_{rxn}}{RT} \right) \Big|_{T_1}^{T_2}$$

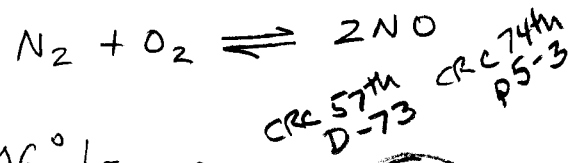
$$\ln(K_{p2}/K_{p1}) = - \frac{\Delta H_{rxn}}{R} \left( \frac{1}{T_2} - \frac{1}{T_1} \right)$$

Example - simple cases

note for complex (Real) mixtures you need a computer code!

$$K_a \equiv \exp\left(-\frac{\Delta G_{rxn}}{RT}\right)$$

G=H-TS



$$\Delta G_{N_2}^{\circ} \Big|_{25^{\circ}C} = 0$$

$$\Delta G_{O_2}^{\circ} \Big|_{25^{\circ}C} = 0$$

CRC 57th D-74

$$\begin{aligned} \Delta G_{rxn}^{\circ} \Big|_{25^{\circ}C} &= 2\Delta G_{NO}^{\circ} - \Delta G_{O_2}^{\circ} - \Delta G_{N_2}^{\circ} \\ &= 2(20.719 \frac{kcal}{mol}) - 0 - 0 \\ &= 41.44 kcal/mol \end{aligned}$$

$$\Delta G_{NO}^{\circ} \Big|_{25^{\circ}C} = 20.719 \frac{kcal}{mol}$$

$$K_p = \exp\left(-\frac{41.44 \frac{kcal}{mol} \left(\frac{10^3 cal}{1 kcal}\right)}{\left(\frac{1.987 cal}{mol \cdot K}\right)(273+25)}\right)$$

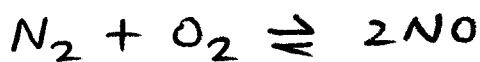
at

20.72  
D-73  
CRC 57th

$$= 4.04 \times 10^{-30} \text{ at } 25^{\circ}C$$

Exists as all O<sub>2</sub> and N<sub>2</sub>

Example Problem: Find  $K_p$  at  $25^\circ\text{C}$



$$\Delta G_{\text{N}_2}^{\circ} \Big|_{25^\circ\text{C}} = 0$$

CRC 57<sup>th</sup> D-73 & 74

$$\Delta G_{\text{O}_2}^{\circ} \Big|_{25^\circ\text{C}} = 0$$

CRC 74<sup>th</sup> p 5-3

$$\Delta G_{\text{NO}}^{\circ} \Big|_{25^\circ\text{C}} = 20.72 \text{ kcal/mol}$$

$$\begin{aligned} \Delta G_{\text{rxn}}^{\circ} &= 2 \Delta G_{\text{NO}}^{\circ} - \Delta G_{\text{N}_2}^{\circ} - \Delta G_{\text{O}_2}^{\circ} = 2(20.72) \text{ kcal/mol} \\ &= 41.44 \text{ kcal/mol} \end{aligned}$$

$$K_p = \exp \left[ - \frac{41.44 \text{ kcal/mol} \left( \frac{10^3 \text{ cal}}{\text{kcal}} \right)}{\left( \frac{6.987 \text{ cal}}{\text{mol K}} \right) (273 + 25) \text{ K}} \right]$$

$$= 4.04 \times 10^{-30} \text{ at } 25^\circ\text{C} \quad \text{exists as all } \text{O}_2 \text{ \& } \text{N}_2 \text{ at } 25^\circ\text{C}$$

CRC 74<sup>th</sup> 5-67 for NO

Find  $K_p$  at  $2700\text{K}$

$$\Delta H_{\text{rxn}}^{\circ} = 2 H_{\text{f NO}}^{\circ} - H_{\text{f O}_2}^{\circ} - H_{\text{f N}_2}^{\circ}$$

$$= 2(21.60 \frac{\text{kcal}}{\text{mol}}) - 0 - 0$$

$$= 43.2 \text{ kcal/mol} \quad \text{Endothermic}$$

Does  $\Delta H_{\text{rxn}}$  change with  $T$ ?

Sandler, CHE Thermo

$$\hat{C}_p = \int_{T_1}^{T_2} c_p dT = a \Delta T + \frac{b}{2} (T_2^2 - T_1^2) + \frac{c}{3} (T_2^3 - T_1^3) + \frac{d}{4} (T_2^4 - T_1^4)$$

	a	b x 10 <sup>2</sup>	c x 10 <sup>5</sup>	d x 10 <sup>9</sup>
NO	6.461	0.2358	-0.07705	0.08729
O <sub>2</sub>	6.732	0.1565	-0.01791	0
N <sub>2</sub>	6.529	0.1488	-0.02271	0

Eq 8-25

$$\Delta C_{p,rxn} = 2 \hat{C}_{p,NO} - \hat{C}_{p,O_2} - C_{p,N_2}$$

$$\int_{298}^{2700} \Delta C_{p,rxn} dT = 2(20,120) - 20,416 - 19,552 = 273 \text{ cal/mol}$$

$$\Delta H_{rxn}/T = \Delta H_{rxn}^{\circ} \Big|_{298K} + \int_{298}^{2700} \Delta C_p dT \quad \text{Eqn 8-26 P. 434}$$

$$\Delta H_{rxn} = 43,200 \text{ cal/mol} + 273 \text{ cal/mol}$$

(average)      this is small  $\therefore \Delta H_{rxn} \approx \text{const.}$

$$\ln \left( \frac{K_{p2}}{K_{p1}} \right) = - \frac{\left( 43,200 + \frac{273}{2} \right)}{1.987 \frac{\text{cal}}{\text{mol K}}} \left[ \frac{1}{2700} - \frac{1}{298} \right]$$

$$K_{p2} = 0.076$$



## PETROCHEMICAL DEVELOPMENTS

# Find favorable reactions faster

Equations for Gibbs free energy will help identify favorable reactions

C. L. Yaws and P.-Y. Chiang, Lamar University, Beaumont, Texas

A RECENT ARTICLE<sup>1</sup> reported equations to help calculate the heat of reaction for proposed organic chemical reactions. In that article, enthalpy equations were given for 700 major organic compounds.

Now, equations are given to identify whether the reactions are thermodynamically favorable. The method uses Gibbs free energy of formation for the reactants and products. The equation for any 700 major organic compounds is given as temperature coefficients. Then the reaction can be tested at various temperature levels beyond the standard 298°K conditions imposed by many other data tabulations. Data for water and hydrogen chloride are also included.

Gibbs free energy of formation of ideal gas ( $\Delta G_f$ , kjoule/g-mol) is calculated from the tabulated coefficients ( $A$ ,  $B$ ,  $C$ ) and the temperature ( $T$ , °K) using the following equation:

$$\Delta G_f = A + BT + CT^2 \quad (1)$$

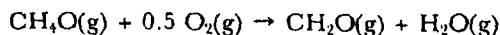
Chemical equilibrium for a reaction is associated with the change in Gibbs free energy ( $\Delta G_r$ ) calculated as follows:

$$\Delta G_r = \Delta G_{f, \text{products}} - \Delta G_{f, \text{reactants}} \quad (2)$$

If the change in Gibbs free energy is negative, the thermodynamics for the reaction are favorable. On the other hand, if the change in Gibbs free energy is highly positive, the thermodynamics for the reaction are not favorable and may be feasible only under special circumstances. Rough criteria for screening chemical reactions are as follows:

$\Delta G_r < 0$ kjoules/g-mol	favorable
$0 < \Delta G_r < 50$ kjoules/g-mol	possibly favorable
$\Delta G_r > 50$ kjoules/g-mol	not favorable

**Example.** Calculate the change in Gibbs free energy for the reaction of methanol and oxygen to produce formaldehyde and water at reaction temperatures of 600, 700, 800, 900 and 1,000°K:



Using correlation constants from Table 1 (see pp. 82-84) and Eq. 1 at temperature of 600°K, we obtain:

$$\Delta G_{f, \text{CH}_2\text{O}} = -115.972 + 1.663 \cdot 10^{-2}(600) + 1.138 \cdot 10^{-5}(600^2) = -101.9$$

$$\Delta G_{f, \text{H}_2\text{O}} = -241.74 + 4.174 \cdot 10^{-2}(600) + 7.428 \cdot 10^{-6}(600^2) = -214.02$$

$$\Delta G_{f, \text{CH}_4\text{O}} = -201.860 + 1.254 \cdot 10^{-1}(600) + 2.035 \cdot 10^{-5}(600^2) = -119.28$$

$$\Delta G_{f, \text{O}_2} = 0$$

The change in Gibbs free energy for the reaction is determined from Eq. 2 and the Gibbs free energy of formation for the products and reactants:

$$\begin{aligned} \Delta G_r &= \Delta G_{f, \text{CH}_2\text{O}} + \Delta G_{f, \text{H}_2\text{O}} - \Delta G_{f, \text{CH}_4\text{O}} - 0.5 \Delta G_{f, \text{O}_2} \\ &= -101.9 + (-214.02) - (-119.28) - 0 \end{aligned}$$

$$= -196.64 \text{ kjoule/g-mol}$$

Repeating the calculations at the other temperatures gives these results:

$T$ , °K	600	700	800	900	1,000
$G_r$ , kJ/g-mol	-197	-204	-210	-217	-224

Since the change in Gibbs free energy for the reaction is highly negative, the thermodynamics for the reaction at these temperatures are favorable (reaction promising).

**Data source.** The correlation constants were determined from a least-squares fit of data from the literature.<sup>2-13</sup> In most cases, average deviations between calculated and reported data were less than 0.6 kjoules/g-mol.

A copy (5¼ inch floppy disk) of a menu-driven computer program to calculate Gibbs free energy of formation and change in Gibbs free energy for reactions (including random access data file of compound coefficients) is available for a nominal fee. For details, contact: C. L. Yaws, Dept. of Chem. Engg., Lamar University, P.O. Box 10053, Beaumont, Texas 77710, USA.

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### The authors

**Carl L. Yaws** is a professor at Lamar University, Beaumont, Texas. Earlier he worked in industrial design, research and production. He is a graduate of Texas A&I University and the University of Houston, and is a registered professional engineer. He holds several patents and is the author of a book and numerous technical papers.



**Pai-Yu (Polly) Chiang** holds an MS degree in chemical engineering from Lamar University, Beaumont, Texas, where the work for this article was performed. She is now working as a chemical engineer for a major process equipment fabricator. Her research interests are in the areas of thermodynamics, environmental engineering and distillation.



TABLE 1—Gibbs free energy of formation of gas, ΔG<sub>f</sub> = A + BT + CT<sup>2</sup>

NO.	FORMULA NAME	A	B	C	DEL GF 2298K	NO.	FORMULA NAME	A	B	C	DEL GF 2298K
1	CCL4 CARBON-TETRACHLORIDE	-100.838	1.4561E-01	-8.6766E-06	-58.24	117	C3H7NO2 1-NITROPROPANE	-127.329	4.1957E-01	2.5482E-05	0.33
2	CCL3F TRICHLOROFLUOROMETHANE	-234.764	1.3487E-01	-5.3707E-06	-245.18	118	C3H7NO2 2-NITROPROPANE	-142.923	4.2813E-01	2.4633E-05	-12.80
3	CCL2F2 DICHLORODIFLUOROMETHANE	-481.626	1.4402E-01	-4.3398E-06	-438.26	119	C3H7NO3 PROPYL-NITRATE	-177.035	4.9531E-01	1.9599E-05	-27.32
4	CCLF3 CHLOROTRIFLUOROMETHANE	-494.327	1.3545E-01	-6.8525E-07	-653.36	120	C3H7NO3 ISOPROPYL-NITRATE	-194.076	5.0799E-01	1.8793E-05	-40.67
5	CF4 CARBON-TETRAFLUORIDE	-933.816	1.5206E-01	-6.7334E-08	-858.43	121	C3H8 PROPANE	-105.403	2.6475E-01	3.2500E-05	-23.47
6	CO CARBON-MONOXIDE	-109.885	-9.2218E-02	1.6547E-06	-137.28	122	C3H8O ETHYL-METHYL-ETHER	-118.142	3.2628E-01	3.2734E-05	-117.65
7	CO2 CARBON-DIOXIDE	-395.360	-8.8212E-03	1.3322E-06	-394.38	123	C3H8O PROPYL-ALCOHOL	-259.317	3.1232E-01	3.3063E-05	-162.97
8	CO3 CARBONYL-SULFIDE	-136.376	-1.0575E-01	2.5162E-06	-145.64	124	C3H8O ISOPROPYL-ALCOHOL	-274.608	3.2915E-01	2.9243E-05	-173.59
9	CS2 CARBON-DISULFIDE	121.242	-1.9750E-01	5.0587E-05	66.90	125	C3H8S ETHYL-METHYL-SULFIDE	-55.315	2.0160E-01	7.3615E-05	11.42
10	CHCL3 CHLOROFORM	-101.846	1.1137E-01	-8.6302E-07	-68.53	126	C3H8S 1-PROPANETHIOL	-63.596	1.9653E-01	7.3301E-05	2.18
11	CHCL2F DICHLOROFLUOROMETHANE	-283.827	1.0295E-01	-3.0690E-06	-252.31	127	C3H8S 2-PROPANETHIOL	-72.284	2.1257E-01	7.0456E-05	-2.55
12	CHCLF2 CHLORODIFLUOROMETHANE	-482.201	1.0493E-01	-4.2461E-06	-450.47	128	C3H9N PROPYLAMINE	-74.693	3.7313E-01	3.2876E-05	39.79
13	CHF3 TRIFLUOROMETHANE	-698.169	1.1520E-01	7.1054E-06	-663.28	129	C3H9N TRIMETHYLAMINE	-26.507	4.0989E-01	3.2215E-05	98.91
14	CH3I TRIIODOMETHANE	116.349	1.0932E-01	-2.3734E-06	177.95	130	CAF8 OCTAFLUOROCCYCLOBUTANE	-1530.065	4.4414E-01	-1.3877E-05	-1398.84
15	CHNS ISOTHIOCYANIC-ACID	129.895	-6.6463E-02	3.1215E-05	112.88	131	CAI2 BUTADIENE(BIACETYLENE)	473.689	-9.9298E-02	-6.8000E-07	443.96
16	CH2CL2 DICHLOROETHANE	-95.965	8.8000E-02	-8.5438E-06	-68.37	132	CAH4 TETRAETHYLENE(VINYLAACETYLENE)	304.509	1.1750E-03	1.1754E-05	305.98
17	CH2CLF CHLOROFLUOROETHANE	-262.549	8.3366E-02	-1.0838E-05	-234.54	133	CAH6 FURAN	-35.958	1.1791E-01	1.7007E-05	0.88
18	CH2F2 DIFLUOROETHANE	-453.610	9.0621E-02	1.2721E-05	-425.35	134	CAH8 TINDOPHENE	118.623	1.2478E-02	4.9100E-05	126.78
19	CH2I2 DIIODOMETHANE	53.545	9.2134E-02	3.1467E-06	101.29	135	CAH6 1,2-BUTADIENE	161.452	1.1686E-01	2.2211E-05	198.45
20	CH2O FORMALDEHYDE	-115.972	1.6630E-02	1.1581E-05	-109.91	136	CAH6 1,3-BUTADIENE	109.172	1.3294E-01	1.9003E-05	158.67
21	CH2O2 FORMIC-ACID	-379.125	9.1431E-02	9.5248E-06	-351.30	137	CAH6 1-BUTYNE(DIETHYLACETYLENE)	164.525	1.1922E-01	2.1726E-05	202.09
22	CH3BR BROMOMETHANE	-55.241	8.0199E-02	1.1207E-05	-28.16	138	CAH6 2-BUTYNE(DIETHYLACETYLENE)	145.727	1.2497E-01	2.5536E-05	185.48
23	CH3CL CHLOROMETHANE	-84.903	7.5722E-02	1.4823E-05	-42.89	139	CAH6 CYCLOBUTENE	128.171	1.4815E-01	2.4315E-05	174.72
24	CH3F FLUOROMETHANE	-234.475	7.6613E-02	1.6807E-05	-209.99	140	CAH6O3 ACETIC-AMIDRIDE	-578.076	3.3162E-01	2.5188E-05	-476.68
25	CH3I IODOMETHANE	-20.627	8.3254E-02	8.0701E-06	15.45	141	CAH7N BUTYRONITRILE	32.613	2.6473E-01	2.5125E-05	108.66
26	CH3NO2 NITROMETHANE	-76.173	2.2734E-01	1.4355E-05	-6.95	142	CAH7N ISOBUTYRONITRILE	23.812	2.5960E-01	2.4170E-05	103.60
27	CH3NO2 METHYL-NITRITRIDE	-65.640	2.2023E-01	9.2945E-06	1.00	143	CAH8 1-BUTENE	-1.692	2.3442E-01	3.1582E-05	71.30
28	CH3NO3 METHYL-NITRATE	-122.358	3.0626E-01	8.2197E-06	-30.17	144	CAH8 2-BUTENE,CIS	-8.619	2.3793E-01	3.6144E-05	65.86
29	CH4 METHANE	-75.262	7.5925E-02	1.8700E-05	-50.84	145	CAH8 2-BUTENE,TRANS	-12.497	2.4252E-01	3.2484E-05	62.97
30	CH4O METHANOL	-201.860	1.2542E-01	2.0345E-05	-162.51	146	CAH8 2-METHYLPROPENE	-18.295	2.4609E-01	3.0860E-05	58.07
31	CH4S METHANETHIOL	-19.483	1.6198E-02	5.2738E-05	-9.92	147	CAH8 CYCLOBUTANE	24.216	2.7677E-01	3.3570E-05	110.04
32	CH5N METHYLAMINE	-26.115	1.8179E-01	2.2182E-05	32.26	148	CAH8BR2 1,2-DIBROMOBUTANE	-135.879	3.9161E-01	1.6038E-05	-13.14
33	CH2CL4 TETRACHLOROETHENE	-12.176	1.1919E-01	-7.6720E-06	22.54	149	CAH8BR2 2,3-DIBROMOBUTANE	-139.240	4.0686E-01	1.5194E-05	-11.92
34	CH2CL6 HEXACHLOROETHANE	-142.168	2.9199E-01	-1.8349E-05	-56.82	150	CAH8I2 1,2-DIICHOLOBUTANE	-58.978	3.9654E-01	1.1910E-05	82.09
35	CH2Cl3F3 1,1,2,2,2-PENTACHLORO-1,1,2,2,2-FLUOROETHANE	-696.127	2.7082E-01	-1.6970E-05	-617.14	151	CAH8 BUTYRALDEHYDE	-206.702	2.9866E-01	2.9382E-05	-114.77
36	CH2Cl2F2 1,1,1,2,2-DICHLORO-1,1,2,2,2-FLUOROETHANE	-808.420	2.8167E-01	-1.2046E-05	-805.42	152	CAH8 2-BUTANONE	-339.887	3.0451E-01	3.0949E-05	-144.06
37	CH2ClF2 1,1,2,2,2-PENTACHLORO-1,1,2,2,2-FLUOROETHANE	-1108.399	2.8235E-01	-6.2604E-06	-1025.08	153	CAH8O2 P-DIOXANE	-318.550	5.5161E-01	3.0870E-05	-180.79
38	CH2F4 TETRAFLUOROETHENE	-858.653	1.1776E-01	-1.8959E-05	-623.71	154	CAH8O2 ETHYL-ACETATE	-444.940	3.8444E-01	2.9614E-05	-327.40
39	CH2F6 HEXAFLUOROETHANE	-1344.410	2.9411E-01	-7.6749E-06	-1257.38	155					

Table with columns: NO., FORMULA NAME, A, B, C, DEL GF 3295K. Contains chemical data for various compounds including benzene, toluene, and various alkanes.

Table with columns: NO., FORMULA NAME, A, B, C, DEL GF 3295K. Contains chemical data for various compounds including benzene, toluene, and various alkanes.

Continued

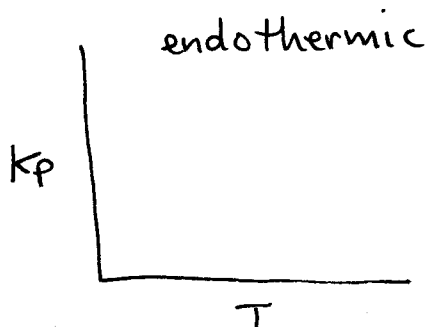
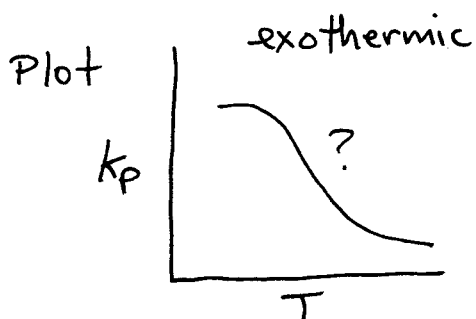


## 8.4 Equilibrium Conversion

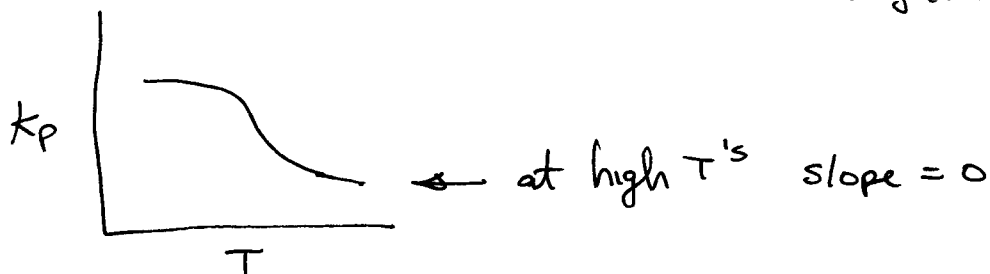
you want highest  $X_{eq}$  ← Goal

Van't Hoff equation  $\frac{d \ln K_p}{dT} = \frac{\Delta H_{rxn}}{RT^2}$

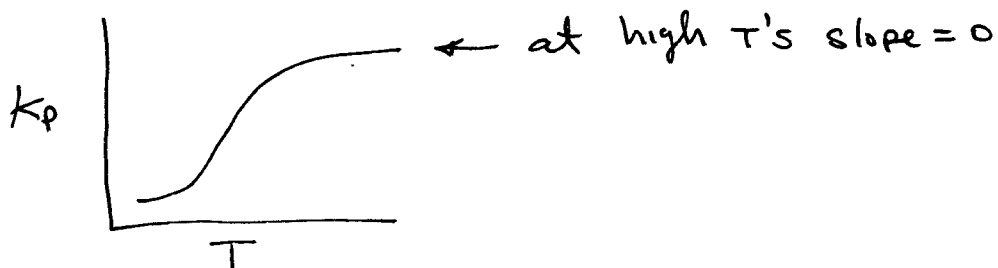
$$K_p \equiv \frac{\text{Products}}{\text{Reactants}}$$



Answer:  $\frac{d \ln K_p}{dT}$  is the slope for exothermic  $\Delta H_{rxn} < 0$   
so slope is negative



Endothermic  $\Delta H_{rxn} > 0$  slope is positive

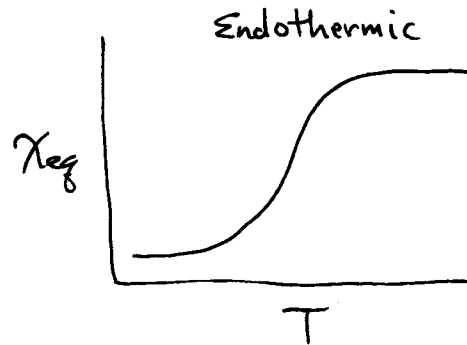
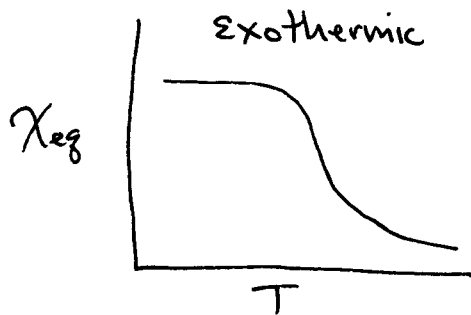




Now Relate  $K_p$  to  $X_{eq}$

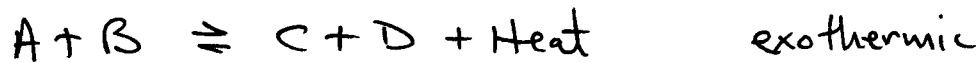
$$K_p = \frac{\text{products}}{\text{Reactants}}$$

$K_p$  is high  $X_{eq}$  is high



OR

Le Chatelier's Principle



As you add heat the rxn  $X$  decreases slows down.

If you remove heat  $X$  increases



If you add heat you get a higher  $X$

(Sandler Thermo

# 8.4 Equilibrium Conversion

$$k = A \exp\left[\frac{42152}{RT}\right] ?$$

For Endothermic

is the equilibrium  $X_{eq}$  with Reversible Reactions  $\nu_{max}$

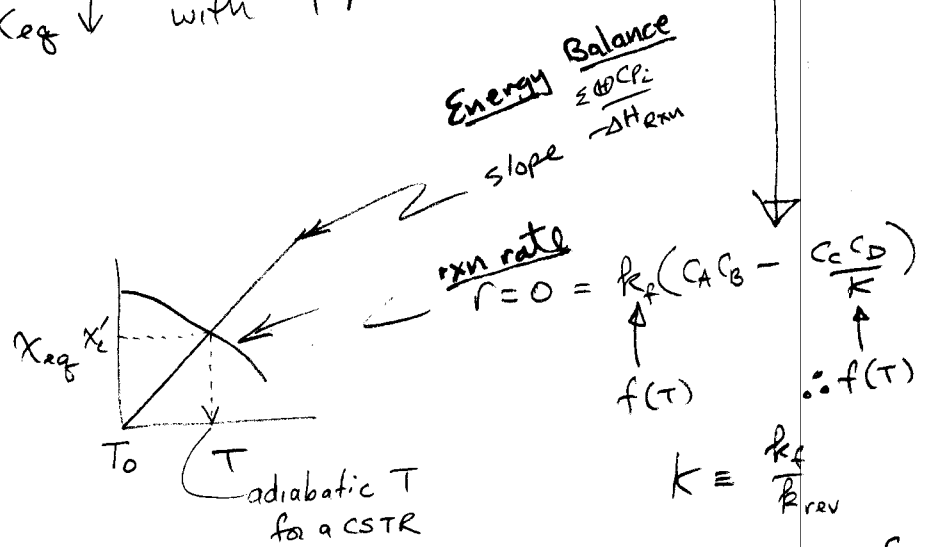
$$r = k(C_A C_B - \frac{C_C C_D}{K_{eq}})$$

Exothermic

$X_{eq} \downarrow$  with  $T \uparrow$

## 8.4.1 $\phi = 0$

Exothermic



Energy Balance

solving for X =

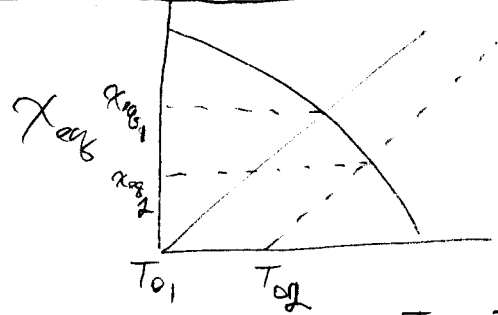
$$X = \frac{\sum \Theta_i \tilde{C}_{p,i} (T - T_0)}{-\left[ \underbrace{\Delta H_{rxn}^0}_{-\Delta H_{rxn}|_T} + \Delta \tilde{C}_p (T - T_R) \right]}$$

see aside in PFR

$$X = \left( \frac{\sum \Theta_i \tilde{C}_{p,i}}{-\Delta H_{rxn}} \right) (T - T_0)$$

- from 8-41
- ②  $k_p = k_c (RT)^{\sum \nu_i}$
  - ①  $k_p = \frac{P_c^{\nu_c} P_d^{\nu_d}}{P_A^{\nu_A} P_B^{\nu_B}}$
  - ③ van't Hoff Relation  $\frac{d \ln k_p}{dT} = \frac{\Delta H_{rxn}|_T}{RT^2}$

Look at Exothermic Rxns



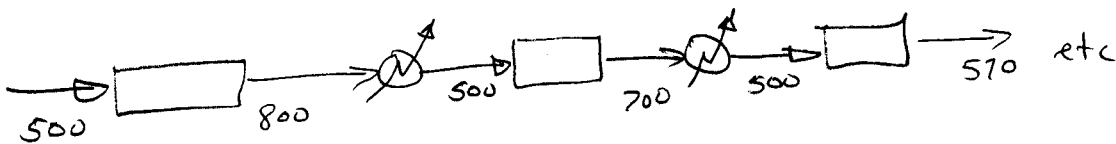
What happens if  $T_0$  increases 8.4.2

if  $\Delta H_{rxn}$  does not vary in the temperature range  $(T - T_0)!$   
not stated in book

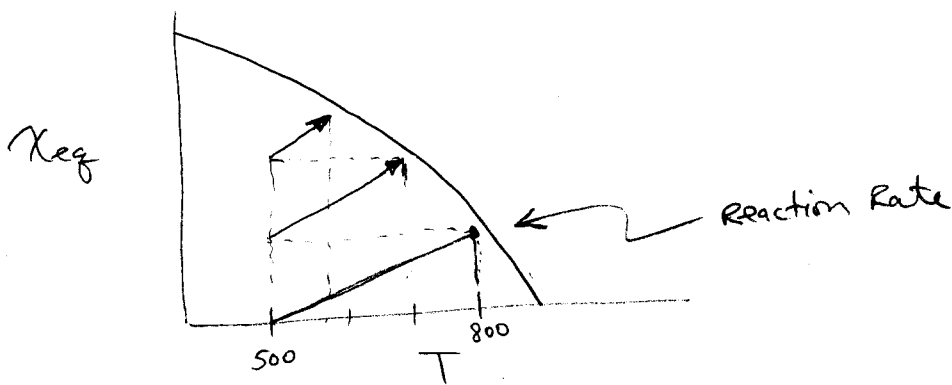
$T_{02} > T_{01}$  (Increase entering fluid Temp)  
 $X_{eq2} < X_{eq1}$

# Interstage Cooling

Higher conversions



Exothermic



## Endothermic

Interstage heating  
upgrading crude oil  
dehydrogenation

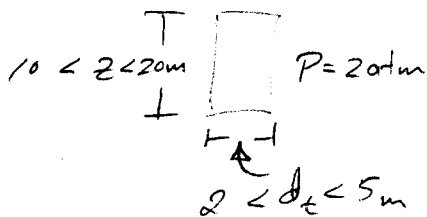
$$430 < T < 530$$

NO Rxn      side Rxn

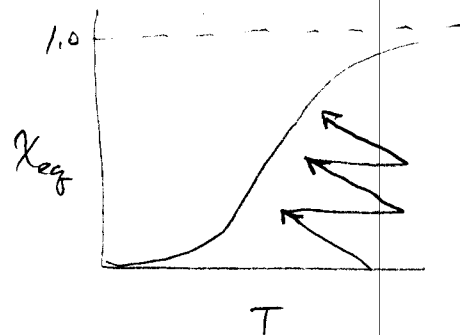
Straight chain  
Alkanes

→ Aromatics

Endo

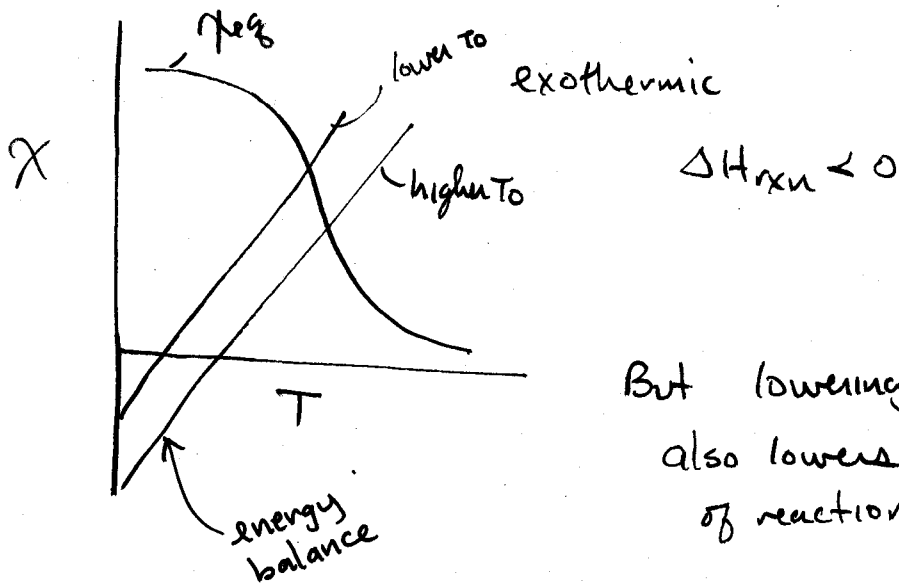


{ Million \$ of Catalyst }  
per reactor



DISCUSS :

Approximate methods for adiabatic reactors  
equilibrium limited.



But lowering the  $T_0$   
also lowers the rate  
of reaction

$$X = \frac{\sum \frac{F_{i0}}{F_{A0}} \tilde{C}_p (T - T_0)}{-\Delta H_{rxn}}$$

$$= T \left( \frac{\sum F_{i0} C_{pi}}{F_{A0} (-\Delta H_{rxn})} \right) + \left( \frac{\sum F_{i0} C_{pi}}{F_{A0} \Delta H_{rxn}} \right) T_0$$

$T_0$  small  
then intercept  
is a small  
negative  
number

if  $T_0$   
large  
Intercept  
large  
Negative  
number

Unsteady-state  $\neq$  multiple steady-states  
8.6

Read 8.5  $\text{SO}_2 + \frac{1}{2}\text{O}_2 \xrightarrow{\text{V}_2\text{O}_5} \text{SO}_3$

$$\rho_b = (33.8 \text{ lbm/ft}^3) \left( \frac{0.4535 \text{ kg}}{\text{lbm}} \right) \left( \frac{\text{ft}}{0.3048 \text{ m}} \right)^3$$

$$= 541.9 \text{ kg/m}^3$$

Example of interstage cooling

## 8.6 Multiple Steady-states

Objective: predict the stable operation of a CSTR

~~8.6.1~~

8.7 Nonisothermal Multiple Rxns  
presented before

8.5 - 8.7

Unsteady-state and multiple steady-states

Multiple steady-states - 8.7

CSTR :

$$V \sum_{i=1}^n C_{p_i} C_i \frac{dT}{dt} = UA(T_a - T) - W_s - F_{A0} \sum_{i=1}^n \frac{F_{i0}}{F_{A0}} \dot{C}_{p_i} (T - T_0) - \Delta H_R |_{T} (-r_A V)$$

Steady state

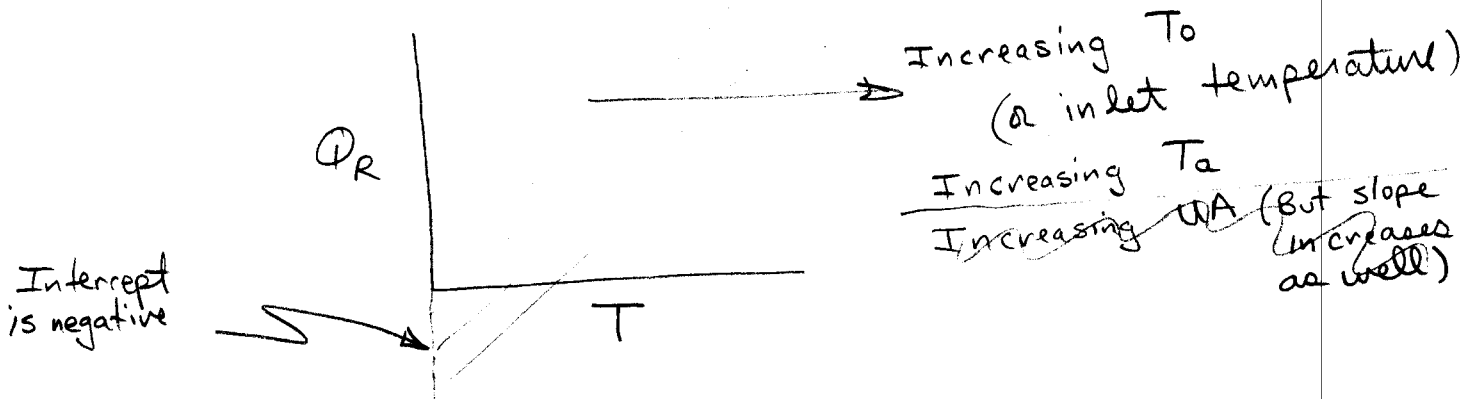
$$\frac{d(\rho_i V)}{dt} = F_{A0} - F_A + r_A V$$

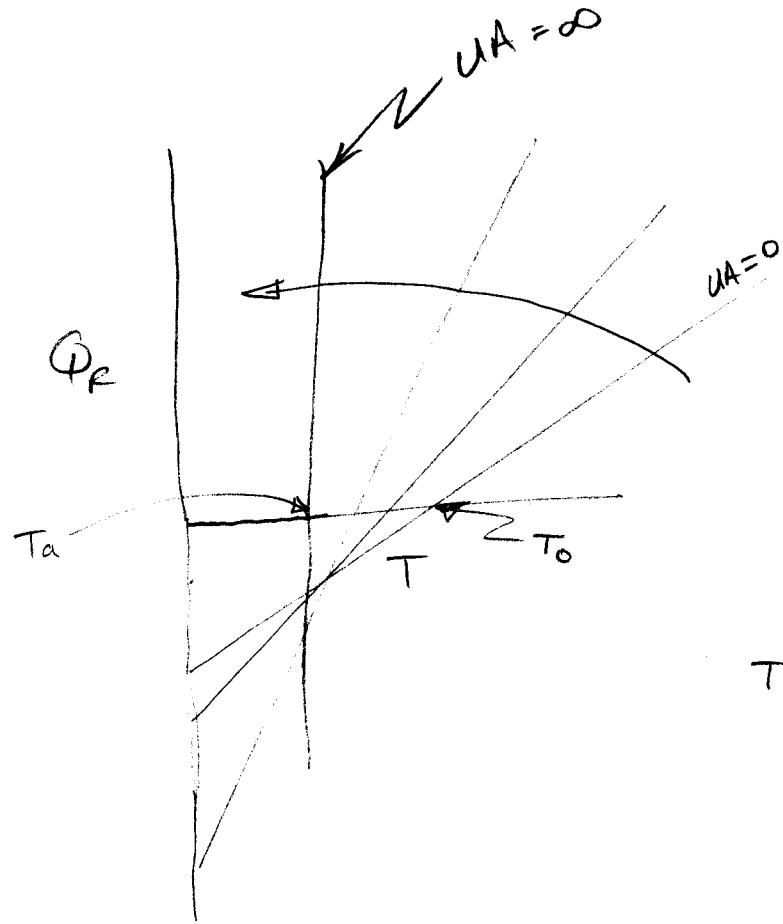
Set  $W_s = 0$

$F_{A0} X_A = F_{A0} - F_A$  By definition

$$UA(T - T_a) + \underbrace{\sum_{i=1}^n F_{i0} \dot{C}_{p_i} (T - T_0)}_{\text{Heat "Removed" } \Phi_R} = \underbrace{\Delta H_R (r_A V)}_{\text{Heat generated } Q_{gen}}$$

$$T \left[ \underbrace{UA + \sum_{i=1}^n F_{i0} \dot{C}_{p_i}}_{\text{slope}} \right] - \underbrace{T_a UA - \sum_{i=1}^n F_{i0} \dot{C}_{p_i} T_0}_{\text{intercept}} = \Delta H_R (r_A V)$$





Increasing UA changes slope and intercept

Note  $Q_R = 0$

$$T = \frac{(\sum F_{i0} C_{p_i}) T_0 + UA T_a}{\sum F_{i0} C_{p_i} + UA}$$

at  $UA = 0$

$$T = T_0$$

at  $UA \gg \sum F_{i0} C_{p_i}$  ( $UA = \infty$ )

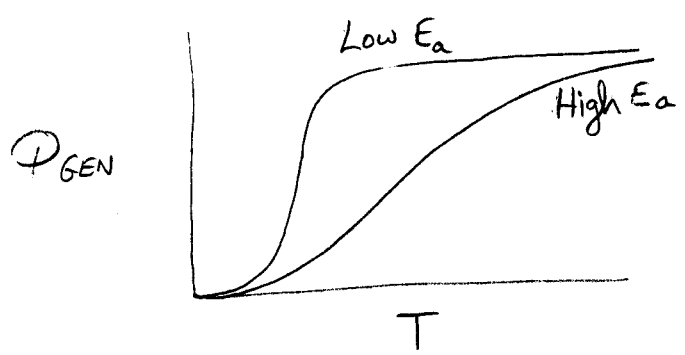
$$T = T_a$$

for  $T_a < T_0$   
 ( $T_a$  is used for cooling)

Heat generation :

$$\Delta H_{Rxn} V = \Delta H_{Rxn} (-k f(c)) V$$

$$A \exp\left(-\frac{E}{RT}\right)$$



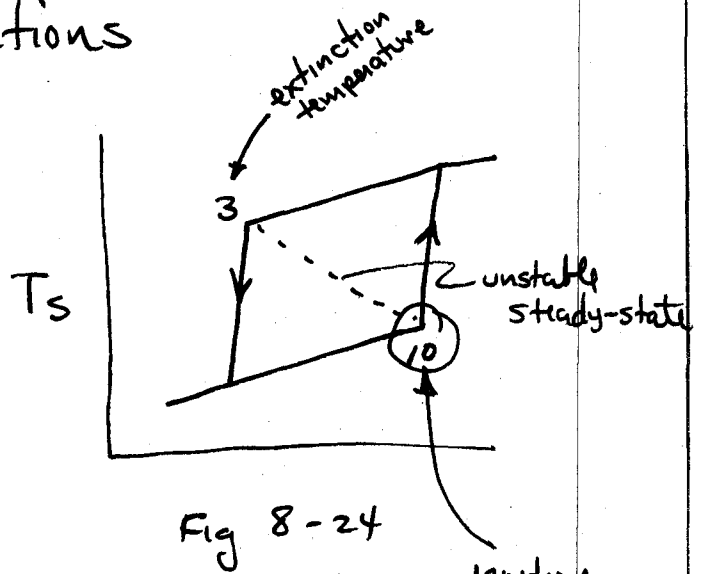
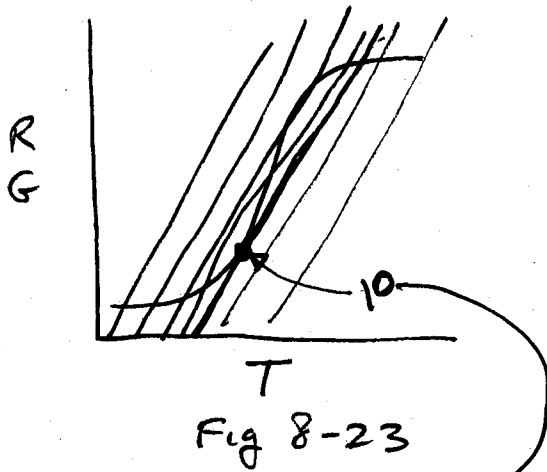
$$\frac{A}{\exp(E/RT)}$$

$T \rightarrow \infty \Rightarrow A$   
 $T \rightarrow \text{small} \Rightarrow 0$

$$\exp\left(-\frac{E_{High}}{RT}\right) \text{ vs } \exp\left(-\frac{E_{Low}}{RT}\right)$$

$\frac{1}{\exp(+\frac{1600}{T})}$  increases the change  
 $\frac{1}{\exp(+\frac{1}{T})}$  delays the change

# 8.6.4 Runaway Reactions



equation ~~8-77~~ <sup>8-71</sup>  $\frac{dG}{dT} = \frac{dR}{dT}$  equal slopes  
 $-\frac{dn}{dT} = \frac{E}{RT^2}(-r_A)$

ignition temperature giving a jump in rxn Temp

$$\Delta T_{rc} = T_r - T_c = \frac{R T_r^2}{E} \quad \left. \vphantom{\Delta T_{rc}} \right\} \text{Back of the envelope}$$

$T_c$  given by 8-66 page 491 (a mess) =  $\frac{T_0 F_{A0} C_{p0} + UA T_0}{UA + C_{p0} F_{A0}}$

$T_r$  = CSTR reactor temperature

if the reactor temperature rises to 10 then runaway occurs or if  $T_r - T_c > \Delta T_{rc}$  then runaway occurs.

$$C_{p0}(1+k)(T-T_c) = \frac{-r_A V}{F_{A0}} - \Delta H_{rxn} \quad \leftarrow 8-67$$

$$C_{p0}(1+k) = \frac{E}{RT^2} (-r_A) \frac{-\Delta H_{rxn}}{F_{A0}} \quad \leftarrow 8-76$$

$$T - T_c = \frac{RT^2}{E}$$

$$16 < \frac{E}{RT} < 24$$

$$300 < T < 500K$$

$$\Delta T \sim \underline{\underline{15 \text{ to } 30^\circ C}}$$

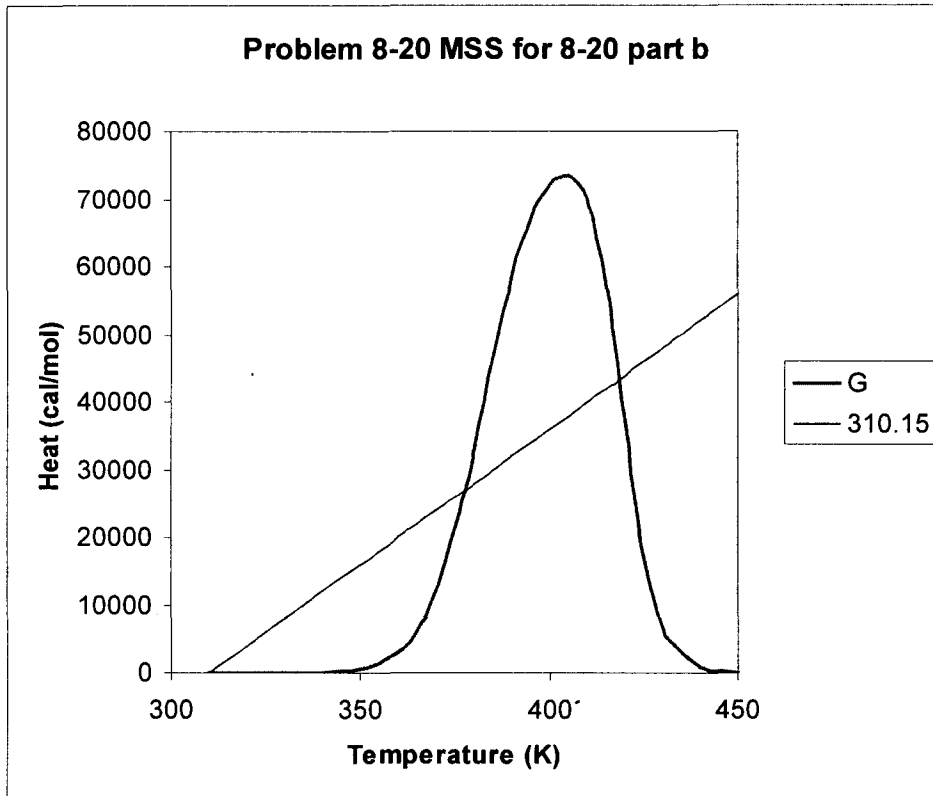




# Steady-state CSTR 49/52

$A \rightleftharpoons B$  liquid phase

Problem 8-~~1b~~ 8-20  
The steady-state temperatures are



On the Spreadsheet the values can be found by trial and error or the solver to give

*Steady State Temps* →

Part b)  $T = 310.2, 377.5, \text{ and } 418.4 \text{ K}$

Part c)  $T = 310.2 \text{ and } 418.4 \text{ K}$  are stable and  $377.5 \text{ K}$  is unstable.

Part d) the conversion corresponding to  $T = 418.4 \text{ K}$  is  $x_A = 0.54$

$$UA(T_g - T) - F_{A0}C_{PA}(T - T_0) = \Delta H_{rxn} F_{A0} x_A$$

↑  
Plug in m.B. solution

8-20 e)

Determine MSS

$$T_0 = 310.15K$$

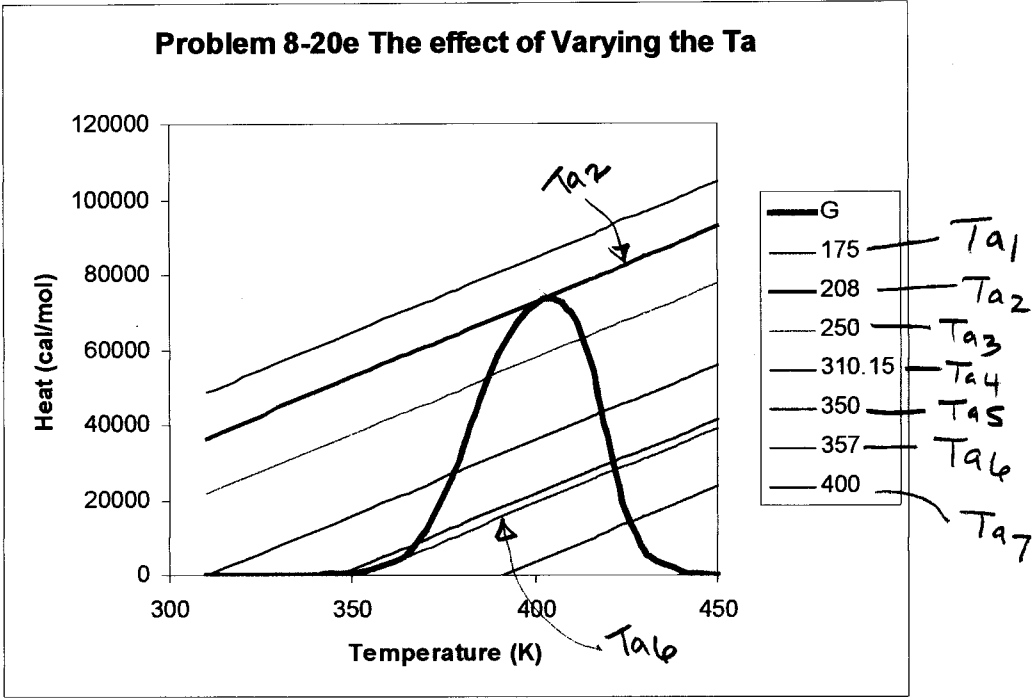
	$T_A (K)$	$T_L$	$T_m$	$T_H$	
$T_{a1}$	175	188.5	-	-	1 soln
$T_{a2}$	208	218.2	190	-	2 soln
$T_{a3}$	250	256	387	413	3 soln
$T_{a4}$	310.15	310.2	377.5	418.4	
$T_{a5}$	350	347	367.5	421.4	
$T_{a6}$	357	357.2	361.2	421.9	2 solns
$T_{a6}'$			361	422.8	
$T_{a7}$	400	-	-	426	1 soln
$T_{a8}$	310	229.6	399.7	403.8	
$T_{a8}$	410			430?	

for  $UA=0$ 

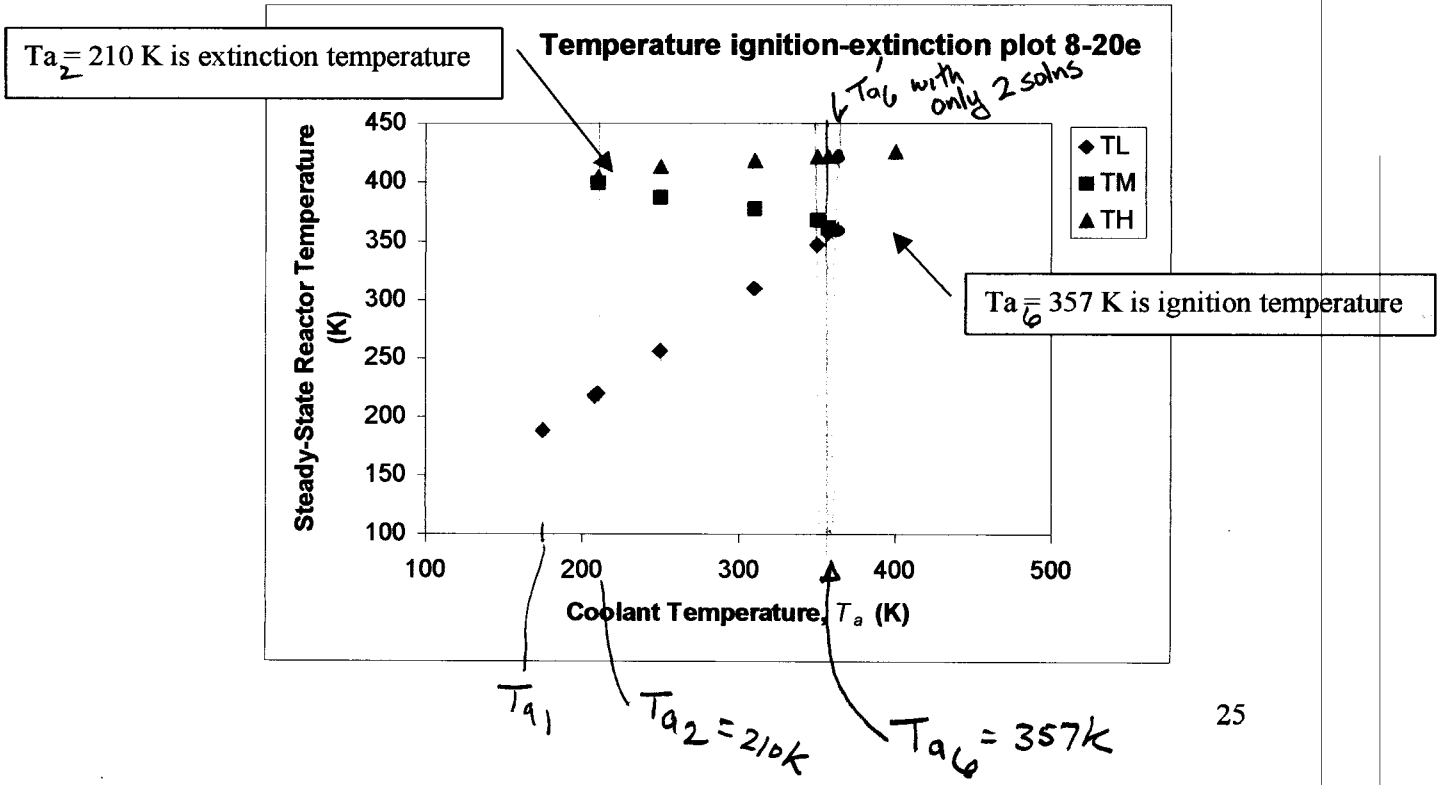
$T_L$  310    431    357K  
                       
           stable    unstable

at  $T=431$ 
 $X_A = 0.061 \leftarrow$  this is an equilibrium conversion

Problem 8-20 part e



In these simulations the lines for the heat removal term R are parallel. The ignition and the extinction temperatures are determined from the analysis which will either blow out the temperature or ignite the reactor temperature.



## Design Project

Thursday:Bring  $C_p$ 's } for each component  
 $\Delta H_f$ Calc.  $\Delta H_{rxn}$  for each reactionStart with using average  $C_p$  values.(this may be all you need) - you will need to justify  
this from a hand or spreadsheet  
calculation

$$\frac{dT}{dV} = \frac{U_a (T_a - T) + \sum_{i=1}^{\mathcal{R}} (+r_{ij}) (\Delta H_{rxn ij})}{\sum_{j=1}^M F_j C_{p_j}}$$

M # of j components

 $\mathcal{R}$  # of i rxns8-76  
page 544

End of class we will have a working energy balance.

