

Kinetic Rate in a PFR Reactor: HYSYS

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In this session you will learn how to install a tubular reactor in HYSYS with a kinetic reaction rate. This HYSYS reaction rate will allow specification of an irreversible reaction. We will ignore equilibrium in this tutorial.

The references for this section are taken from the 2 HYSYS manuals:

Simulation Basis: Chapter 4 Reactions

Steady-State Modeling: Chapter 9 Reactors

Reactors.

Taken from: 9.7 Plug Flow Reactor (PFR) Property View

The PFR (Plug Flow Reactor, or Tubular Reactor) generally consists of a bank of cylindrical pipes or tubes. The flow field is modeled as plug flow, implying that the stream is radially isotropic (without mass or energy gradients). This also implies that axial mixing is negligible.

As the reactants flow the length of the reactor, they are continually consumed, hence, there will be an axial variation in concentration. Since reaction rate is a function of concentration, the reaction rate will also vary axially (except for zero-order reactions).

To obtain the solution for the PFR (axial profiles of compositions, temperature, etc.), the reactor is divided into several subvolumes. Within each subvolume, the reaction rate is considered to be spatially uniform.

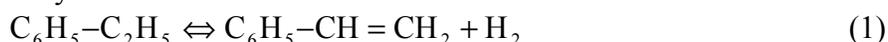
You may add a Reaction Set to the PFR on the Reactions tab. ***Note that only Kinetic, Heterogeneous Catalytic and Simple Rate reactions are allowed in the PFR.***

Reaction Sets (portions from Simulation Basis: Chapter 4 Reactions)

Reactions within HYSYS are defined inside the Reaction Manager. The Reaction Manager, which is located on the Reactions tab of the Simulation Basis Manager, provides a location from which you can define an unlimited number of Reactions and attach combinations of these Reactions in Reaction Sets. The Reaction Sets are then attached to Unit Operations in the Flowsheet.

HYSYS PFR Reactors using kinetic rates– Tutorial using Styrene

Styrene is a monomer used in the production of many plastics. It has the fourth highest production rate behind the monomers of ethylene, vinyl chloride and propylene. Styrene is made from the dehydrogenation of ethylbenzene:



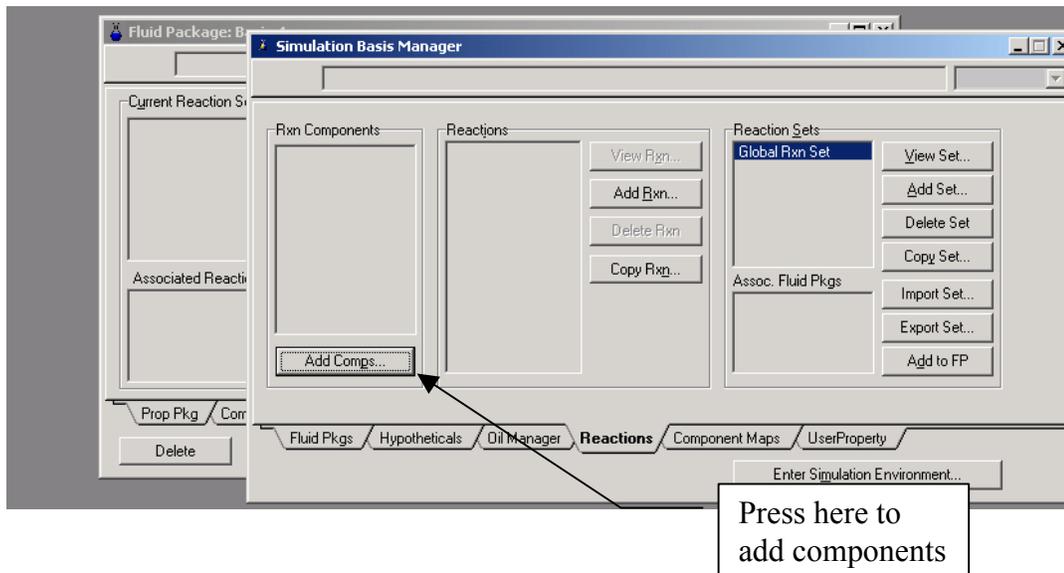
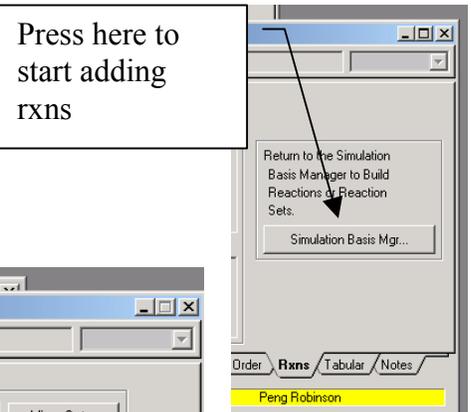
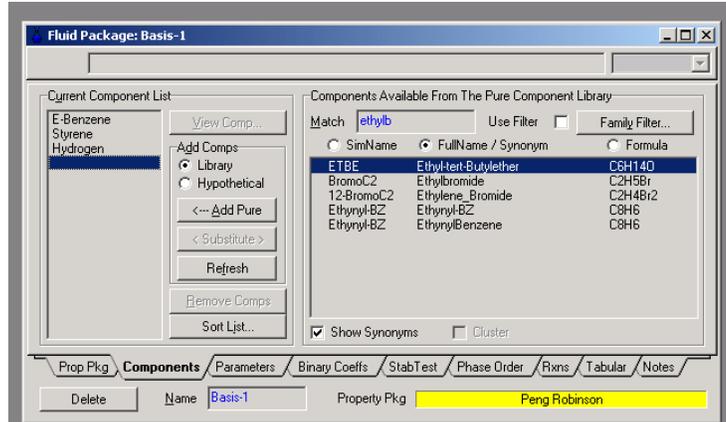
In this reactor we will neglect the aspect that reaction 1 is an equilibrium reaction and model this system using a power law expression. In HYSYS this is called a ***Kinetic Rate*** expression. The reaction rate expression that you will install is given by the following:

$$r_{EB} = -4.24 \times 10^3 \frac{\text{mol EB}}{\text{L}_{\text{reactor}} \text{ kPa s}} p_{EB} \exp \left[- \frac{21708 \text{ cal/mol}}{\left(1.987 \frac{\text{cal}}{\text{mol K}} \right) T} \right] \quad (2)$$

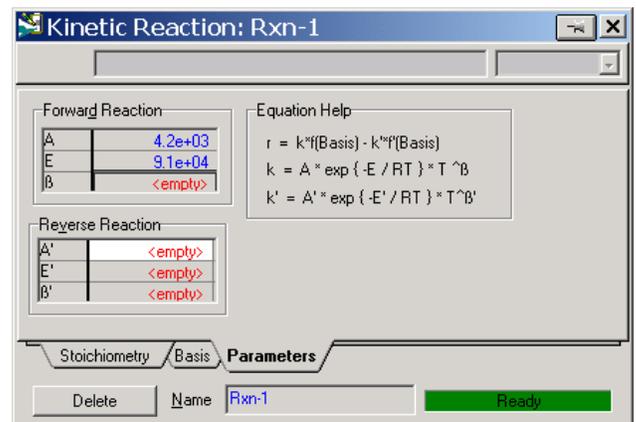
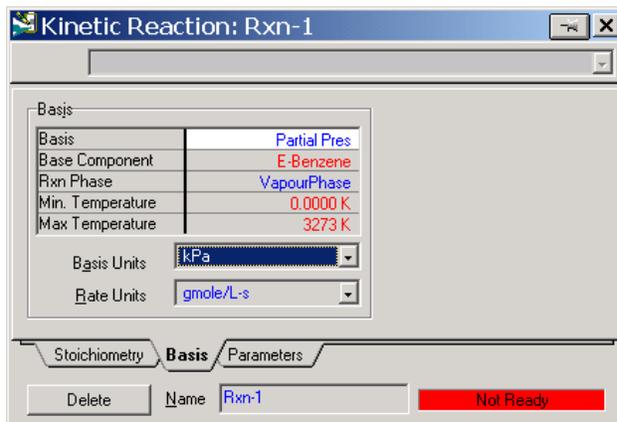
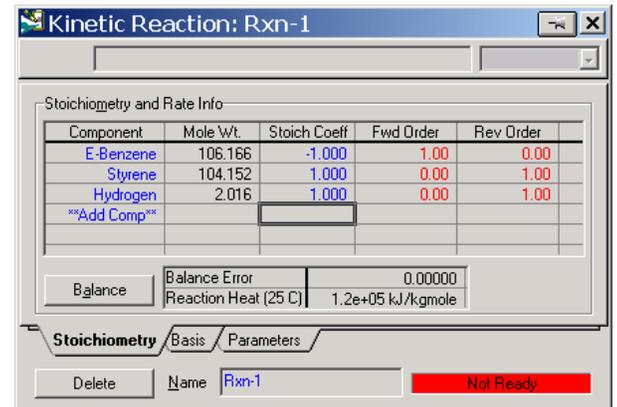
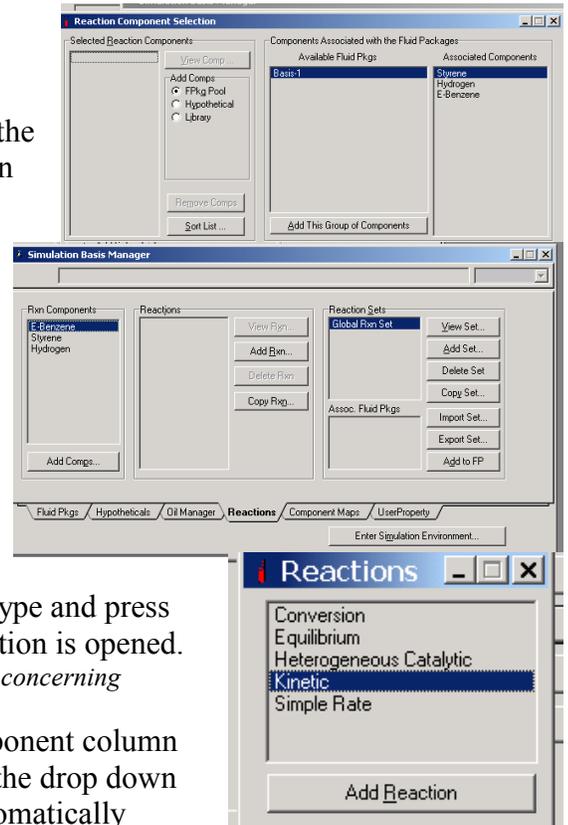
Notice that the reaction rate has units and that the concentration term is partial pressure with units of kPa.

Procedure to Install a Kinetic Reaction Rate:

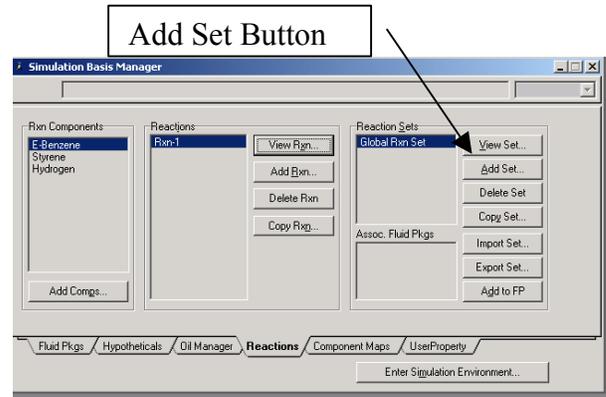
1. Start HYSYS
2. Since these compounds are hydrocarbons, use the Peng-Robinson thermodynamic package. *(Additional information on HYSYS thermodynamics packages can be found in the Simulation Basis Manual Appendix A: Property Methods and Calculations. Note an alternative package for this system is the PRSV)*
3. Install the chemicals for a styrene reactor: ethylbenzene, styrene, and hydrogen. If they are not on this list then use the Sort List... button feature.
4. Now return to the Simulation Basis Manager by either closing the Fluid Package Basis-1 window or clicking on the Rxns tab and pressing the Simulation Basis Mgr... button.
5. On the Reactions tab of the Simulation Basis Manager, press the Add Comps button.



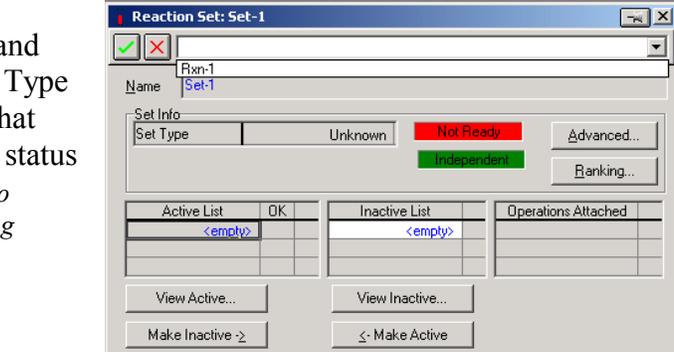
- The Reaction Component Selection view will appear. In the Add Comps group, ensure that the FPkg Pool radio button is selected. This will make only the Fluid Package components available to the Reaction Manager.
- Highlight the Fluid Package in the Available Fluid Pkgs group.
- Press the *Add This Group of Components* button to transfer the fluid package components into the Selected Reaction Components group.
- Press the *Close* button to return to the Reactions tab. The selected components are present in the Rxn Components group.
- To install a reaction, press the *Add Rxn* button.
- From the Reactions view, highlight the Kinetic reaction type and press the Add Reaction button. The property view for the Reaction is opened. Refer to Section 4.4 of the Simulation Basis Manual for information concerning reaction types and the addition of reactions.
- On the Stoichiometry tab select the first row of the Component column in Stoichiometry Info matrix. Select **ethylbenzene** from the drop down list in the Edit Bar. The Mole Weight column should automatically provide the molar weight of ethylbenzene. In the Stoich Coeff field enter -1 (i.e. 1 moles of ethylbenzene will be consumed).
- Now define the rest of the Stoichiometry tab as shown in the adjacent figure. Go to Basis tab and set the Basis as partial pressure, the base component as ethylbenzene and have the reaction take place only in the vapor phase. The pressure basis units should be kPa and the units of the reaction rate were given above as mol/(L s). Since the status bar at the bottom of the property view shows **Not Ready**, then go to the Parameters tab.
- Add the pre-exponential – no units and the activation energy – with units of cal/mol (which is transformed to kJ/kmol after entry.) Leave β blank or place a zero in the cell. Notice that you don't enter the negative sign with the pre-exponential.



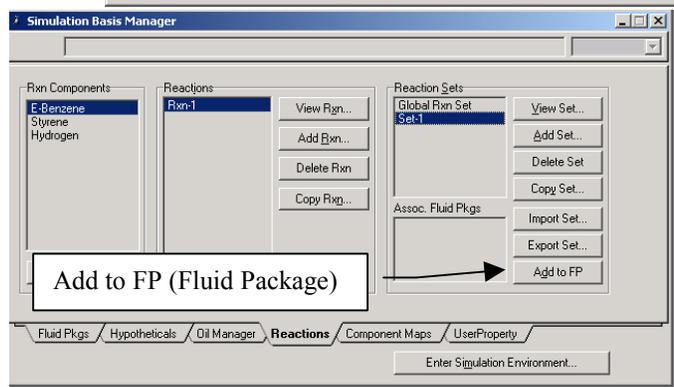
15. Close the property view.
16. By default, the Global Rxn Set is present within the Reaction Sets group when you first display the Reaction Manager. However, for this procedure, a new Reaction Set will be created. Press the Add Set button. HYSYS provides the name Set-1 and opens the Reaction Set property view.
17. To attach the newly created Reaction to the Reaction Set, place the cursor in the <empty> cell under Active List.
18. Open the drop down list in the Edit Bar and select the name of the Reaction. The Set Type will correspond to the type of Reaction that you have added to the Reaction Set. The status message will now display Ready. (Refer to Section 4.5 – Reaction Sets for details concerning Reactions Sets.)
19. Press the Close button to return to the Reaction Manager.



20. To attach the reaction set to the Fluid Package (your Peng Robinson thermodynamics), highlight Set-1 in the Reaction Sets group and press the Add to FP button. When a Reaction Set is attached to a Fluid Package, it becomes available to unit operations within the Flowsheet using that particular Fluid Package.

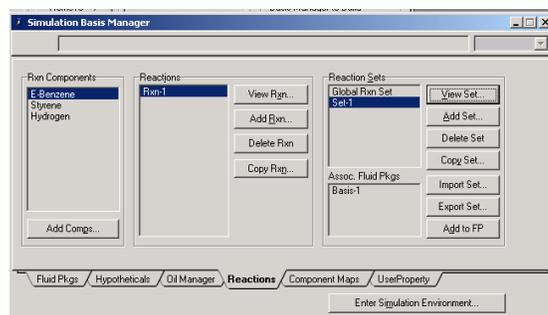


21. The Add 'Set-1' view appears, from



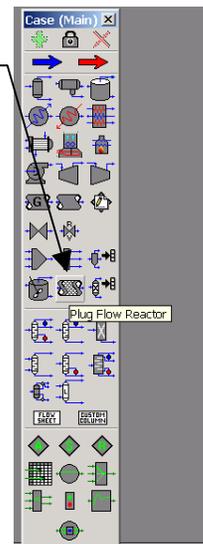
which you highlight a Fluid Package and press the Add Set to Fluid Package button.

22. Press the Close button. Notice that the name of the Fluid Package (Basis-1) appears in the Assoc. Fluid Pkgs group when the Reaction Set is highlighted in the Reaction Sets group.
23. Now Enter the Simulation Environment by pressing the button in the lower right hand portion

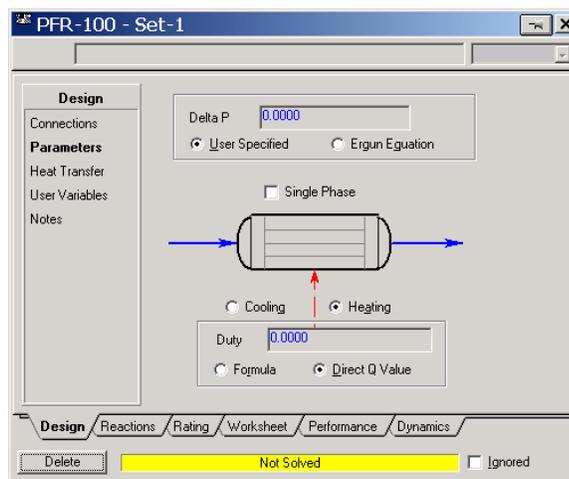
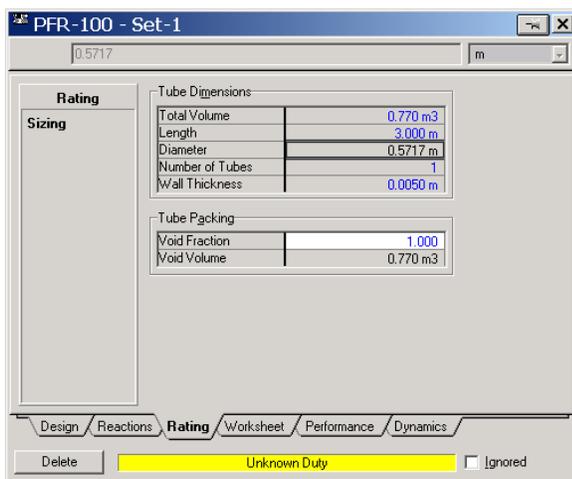
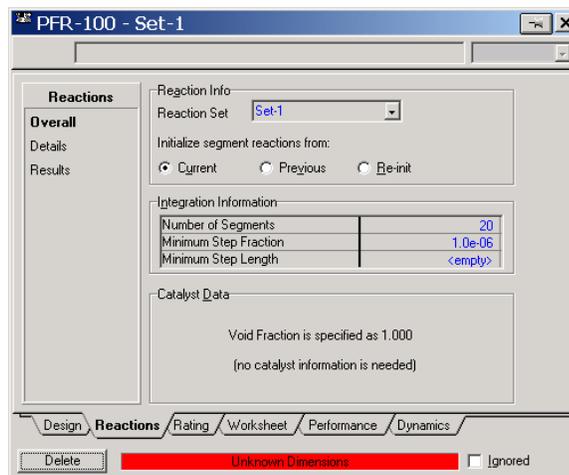
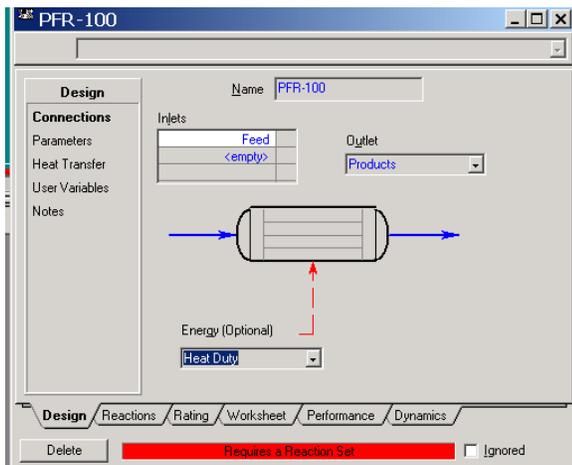


Enter Simulation Environment

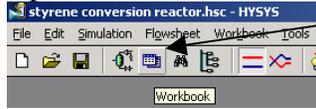
PFR



24. Install a PFR reactor. Either through the
 - 24.1. Flowsheet, Add operation
 - 24.2. f12
 - 24.3. or icon pad. Click on PFR, then release left mouse button. Move cursor to pfd screen and press left mouse button. Double click on the reactor to open.
25. Add stream names as shown. After naming these streams the following errors appear: Requires a Reaction Set and Unknown dimensions.
26. Next add the reaction set by selecting the reactions tab and choosing Reaction Set from the drop down menu.
27. Go to the Ratings Tab. Remember in the case of distillation columns, in which you had to specify the number of stages? Similarly with PFR's you have to specify the volume. In this case add the volume as 0.77 m³ and length 3 m as shown in the figure.
28. Return to the Design tab and specify that this reactor has no pressure drop and is an adiabatic reactor.
29. Close the PFR Reactor



30. Open the workbook



Workbook

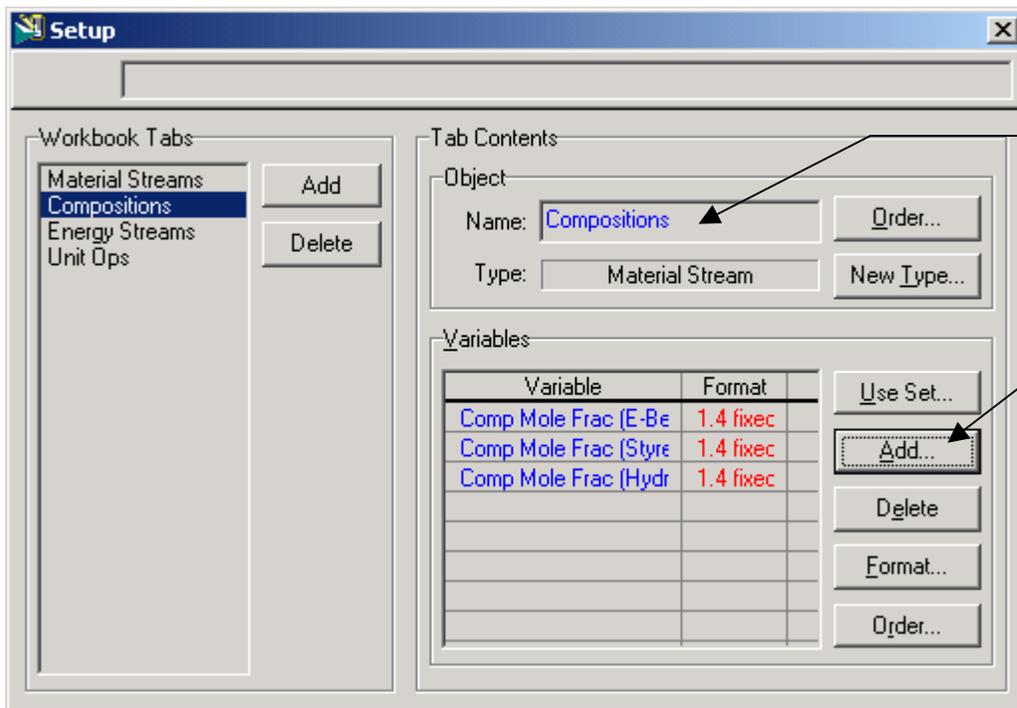
31. Now add a feed composition of pure ethylbenzene at 152.2 gmol/s, 880 K, 1.378 bar.

Remember you can type the variable press the space bar and type or select the units.

32. Isn't it strange that you can't see the molar flowrate in the composition window? Let's add the molar flowrates to the workbook windows. Go to Workbook setup.

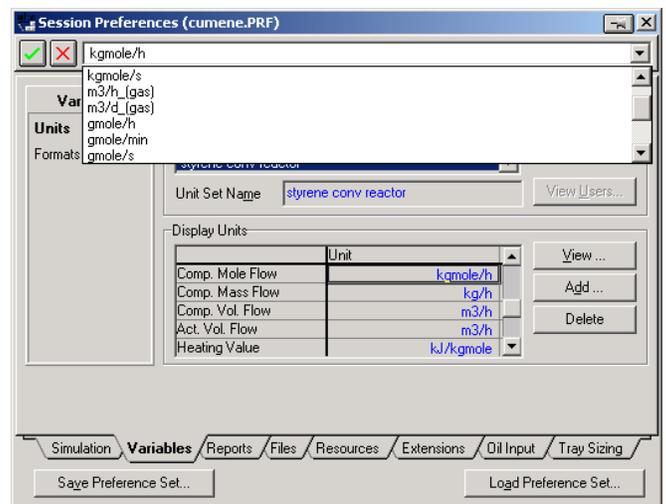
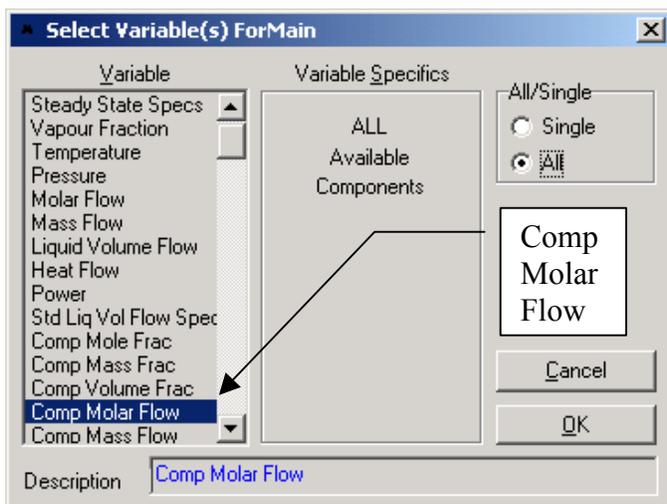
33. Press the Add button on the right side

34. Select Component Molar Flow and then press the All radio button.



Give it a new name such as Compositions

Add Button



35. To change the units of the variables go to Tools, preferences

36. Then either bring in a previously named preference set or go to the variables tab and clone the SI set and give this new set a name.
37. Change the component molar flowrate units from kmol/hr to gmol/s.
38. Change the Flow units from kmol/hr to gmol/s
39. Next change the Energy from kJ/hr to kJ/s.
40. Save preference set as well as the case. Remember that you need to open this preference set every time you use this case.

41. Notice that the reactor has converged after you added the conditions of the feed stream.
42. To run an isothermal reactor you need to delete the duty that was specified (in blue) and specify the outlet temperature. Try it! Isn't that easy!
43. Examine the output in the reactor screens by opening the reactor. Go to the Performance tab and make a plot of the composition profile. Notice that you will have to bring the compositions into the plot.

POLYMATH and Hand Calculations

44. Now we will look at verifying what is going on in HYSYS. Notice that HYSYS is a black box calculation. You can't see what it is doing. Reading the help files will give an indication on how it is integrating the reactor. To fully understand the PFR let's go to some hand calculations given on the following page.

Polymath Setup

$$T = 880 \text{ K}$$

$$r_{EB} = -k P_{EB}$$

$$k = 4.24 \times 10^3 \frac{\text{mol}}{\text{s L kPa}} \exp \left[\frac{-21708 \text{ cal/mol}}{1.987 \frac{\text{cal}}{\text{mol K}} 880 \text{ K}} \right]$$

$$k = 0.017206 \frac{\text{mol}}{\text{s L kPa}}$$

MODEL

$$\frac{dF_{EB}}{dV} = r_{EB}$$

$$F_{EB0} = 152.2 \text{ mol/s}$$

$$\frac{dF_S}{dV} = r_S = -r_{EB}$$

$$F_S = 0$$

$$\frac{dF_H}{dV} = r_H = -r_{EB}$$

$$F_H = 0$$

$$P_0 = 1.378 \text{ Bar} = 1.378 \times 10^5 \text{ Pa} = 137.8 \text{ kPa}$$

$$P_{EB} = \frac{F_{EB}}{F_T} P =$$

$$\Delta P = 0 \quad P_0 = P$$

$$F_T = F_{EB} + F_S + F_H$$

$$V = 0.77 \text{ m}^3 = 770 \text{ L}$$

$$L = 3 \text{ m}$$

Further Sample calculations

$$P_{EB} \Big|_{V=0} = \frac{152.2}{152.2} 137.8 \text{ kPa} = 137.8 \text{ kPa}$$

$$\frac{dF_{EB}}{dV} \Big|_{V=0} \stackrel{\text{MAXRATE}}{=} r_{EB} \Big|_{V=0} = 0.017206 \frac{\text{mol}}{\text{s L kPa}} 137.8 \text{ kPa} = 2.37 \frac{\text{mol}}{\text{L s}}$$

Styrene Simple Rate

2/2

$$\frac{dF_{EB}}{dV} \approx -\frac{(F_{EB} - F_{EB_0})}{V} = 2.37 \text{ mol/Ls}$$

} max rate
assume $r = \text{constant}$
to get an
order of magnitude
value of F_{EB}

$$F_{EB} = 152.2 \frac{\text{mol}}{\text{s}} - 2.37 \frac{\text{mol}}{\text{Ls}} (770 \text{L})$$

= negative number

∴ complete conversion before 770L

45. Construct a POLYMATH program to give the following:

POLYMATH Results

Styrene Kinetic Rate Model 02-20-2002, Rev5.1.230

Calculated values of the DEQ variables

| <u>Variable</u> | <u>initial value</u> | <u>minimal value</u> | <u>maximal value</u> | <u>final value</u> |
|-----------------|----------------------|----------------------|----------------------|--------------------|
| V | 0 | 0 | 770 | 770 |
| FEB | 152.2 | 0.2295141 | 152.2 | 0.2295141 |
| FS | 0 | 0 | 151.97049 | 151.97049 |
| FH | 0 | 0 | 151.97049 | 151.97049 |
| FT | 152.2 | 152.2 | 304.17049 | 304.17049 |
| P | 137.8 | 137.8 | 137.8 | 137.8 |
| T | 880 | 880 | 880 | 880 |
| k | 0.0172065 | 0.0172065 | 0.0172065 | 0.0172065 |
| pEB | 137.8 | 0.103978 | 137.8 | 0.103978 |
| rEB | -2.3710547 | -2.3710547 | -0.0017891 | -0.0017891 |

ODE Report (RKF45)

Differential equations as entered by the user

- [1] $d(\text{FEB})/d(V) = r\text{EB}$
- [2] $d(\text{FS})/d(V) = -r\text{EB}$
- [3] $d(\text{FH})/d(V) = -r\text{EB}$

Explicit equations as entered by the user

- [1] $\text{FT} = \text{FEB} + \text{FS} + \text{FH}$
- [2] $\text{P} = 137.8$
- [3] $\text{T} = 880$
- [4] $k = 4.24e3 * \exp(-21708/1.987/\text{T})$
- [5] $p\text{EB} = \text{FEB}/\text{FT} * \text{P}$
- [6] $r\text{EB} = -k * p\text{EB}$

Comments

- [9] $\text{P} = 137.8$
kPa

Independent variable

variable name : V
initial value : 0
final value : 770

Precision

Step size guess. h = 0.000001
Truncation error tolerance. eps = 0.000001

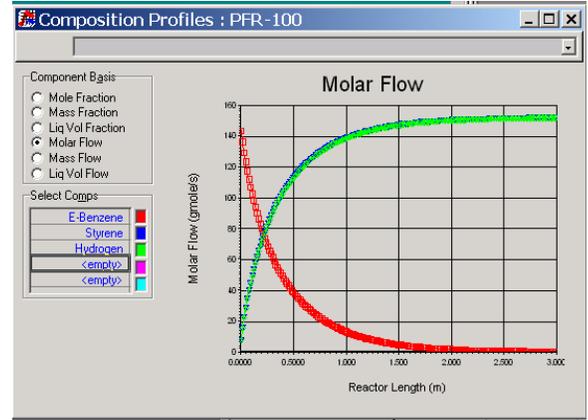
General

number of differential equations: 3
number of explicit equations: 6
Data file: C:\ACdrive\Courses Jan 2002\Reaction Engineering\Lectures&Examples\styrene\styrene kinetic rate model.pol

46. Now let's compare this solution with that given in HYSYS. Notice that the product flowrates of ethylbenzene from POLYMATH is 0.23 mol/s and from HYSYS is 0.55 mol/s. Why is there a difference?

50. Make a plot of the molar flowrates within the PFR.
Go to the Performance tab and click on composition.

At the end of this exercise submit 4 printouts (5 pages total).



- 1) From a word document printout the following (2 pages): **(Paste all of your results into one word document.)** Make the following plots from your Conversion reactor simulation:
 - a) The effect of inlet temperature on the conversion of ethylbenzene for an adiabatic reactor. .
 - b) The effect of reactor temperature on the conversion of ethylbenzene for an isothermal reactor. Hint: you can do this using the Databook. Create a spreadsheet that you can import the feed temperature to a cell B1, then export this temperature from a formula in cell B2 to the product stream. See figures on this page for help.
 - c) POLYMATH program
- 2) On a separate sheet printout the Reaction Summary Printout (See Below for instructions)
- 3) On a separate sheet printout the Reactor Summary Printout

SPRDSHT-1

Current Cell: Exported To: Products, Exportable: B2 Variable: Temperature, Angles in: Rad

| | A | B | C | D |
|---|--------------|--------|---|---|
| 1 | Feed Temp | 1000 K | | |
| 2 | Isothermal T | 1000 K | | |
| 3 | | | | |
| 4 | | | | |
| 5 | | | | |
| 6 | | | | |
| 7 | | | | |
| 8 | | | | |
| 9 | | | | |

Connections Parameters Formulas **Spreadsheet** Calculation Order Files

Delete Function Help... Spreadsheet Only... Ignored

SPRDSHT-1

Spreadsheet Name: SPRDSHT-1

| Cell | Object | Variable Description |
|------|--------|----------------------|
| B1 | Feed | Temperature |

Imported Variables: Edit Import... Add Import... Delete Import

| Cell | Object | Variable Description |
|------|----------|----------------------|
| B2 | Products | Temperature |

Exported Variables: Edit Export... Add Export... Delete Export

Connections Parameters Formulas **Spreadsheet** Calculation Order Files

Delete Function Help... Spreadsheet Only... Ignored

SPRDSHT-1

Spreadsheet Parameters: Number of Columns: 4, Number of Rows: 10, Units Set: styrene

Dynamic Execution: Before Pressure-Flow Step: , After Pressure-Flow Step: , Each Composition Step:

Exportable Cells (Visible in Spreadsheet's Variable List)

| Cell | Visible Name | Variable Name | Variable Type |
|------|-----------------|---------------|---------------|
| B2 | B2: Temperature | Temperature | Temperature |

Connections **Parameters** Formulas Spreadsheet Calculation Order Files

Delete Function Help... Spreadsheet Only... Ignored

SPRDSHT-1

Formula Summary

| Cell | Formula | Result |
|------|---------|--------|
| B2 | +B1 | 1000 K |

Connections Parameters **Formulas** Spreadsheet Calculation Order Files

Delete Function Help... Spreadsheet Only... Ignored

Reaction Summary

1. Go back to the simulation Basis Manager by clicking on the Erlenmeyer flask.
2. View the reaction
3. Remove the pushpin
4. Select File Print and use the preview feature to see the following:
5. Print



Reactor Summary:

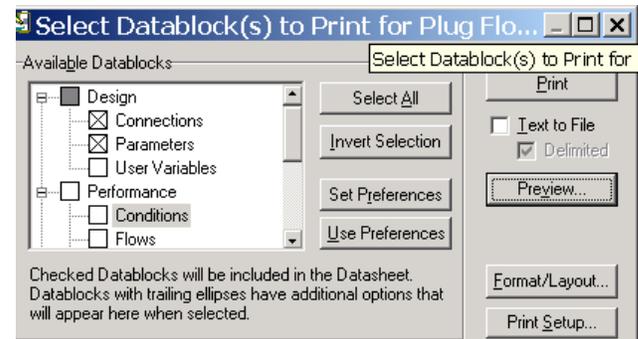
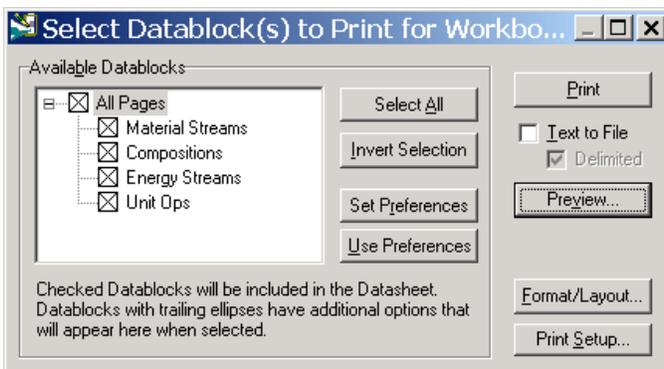
Double click on reactor
Undo pushpin
Select Print from main menu

Then select the Datablock(s) shown in the
Select Datablock(s) to Print for PFR figure:

Workbook

Select workbook and print.

| Rowan University Calgary, Alberta CANADA | | Case Name: C:\ACdrive\Courses Jan 2002\Reaction Engineering\Lectures&Example Unit Set: styrene Date/Time: Wed Feb 20 10:35:22 2002 | | |
|--|------------------|--|---------------|---------------|
| Kinetic: Rxn-1 | | | | |
| STOICHIOMETRY | | | | |
| Component | Molecular Weight | Stoich Coeff | Forward Order | Reverse Order |
| E-Benzene | 106.2 | -1 * | 1.000 | 0.0000 |
| Styrene | 104.2 | 1 * | 0.0000 | 1.000 |
| Hydrogen | 2.016 | 1 * | 0.0000 | 1.000 |
| Balance Error: 0.0000 | | Reaction Heat: 1.176e+005 kJ/kgmole | | |
| BASIS | | | | |
| Basis | Base Component | Rxn Phase | Min. Temp (K) | Max. Temp (K) |
| Partial Pres | E-Benzene | VapourPhase | 0.0000 | 3273 |
| PARAMETERS | | | | |
| Forward Reaction | | Reverse Reaction | | |
| A: 4240 | * | A': --- | | |
| E: 9.083e+004 | * | E': --- | | |



| HYPROTECH | | Rowan University Calgary, Alberta CANADA | Case Name: C:\ACdrive\Courses Jan 2002\Reaction Engineering\Lectures&Example |
|-----------------------------------|--------------------------|--|--|
| | | | Unit Set: styrene |
| | | | Date/Time: Wed Feb 20 10:50:26 2002 |
| Plug Flow Reactor: PFR-100 | | | |
| CONNECTIONS | | | |
| Inlet Stream | | | |
| STREAM NAME | FROM UNIT OPERATION | | |
| Feed | | | |
| Outlet Stream | | | |
| STREAM NAME | TO UNIT OPERATION | | |
| Products | | | |
| Energy Stream | | | |
| STREAM NAME | TO UNIT OPERATION | | |
| Heat Duty | Plug Flow Reactor | | PFR-100 |
| PARAMETERS | | | |
| Physical Parameters | | | |
| Type: User Specified | | | Pressure Drop: 0.0000 kPa * |
| Heat Transfer : Heating | | | |
| Type: Direct Q Value | Energy Stream: Heat Duty | Duty: 6.791e+007 kJ/h | |
| Dimensions | | | |
| Total Volume: | 0.7700 m ³ * | Length: 3.000 m * | Diameter: 0.5717 m |
| Wall Thickness: | 5.000e-003 m * | Void Fraction: 1.0000 * | Void Volume: 0.7700 m ³ |
| Reaction Info | | | |
| Reaction Set: Set-1 | | | Initialize From: Current |
| Integration Information | | | |
| Number of Segments: | 50 * | Minimum Step Fraction: 1.0e-06 * | Minimum Step Length: 3.0e-06 m |

| HYPROTECH | | Rowan University Calgary, Alberta CANADA | Case Name: C:\ACdrive\Courses Jan 2002\Reaction Engineering\Lectures&Example |
|--|-------------------|--|--|
| | | | Unit Set: styrene |
| | | | Date/Time: Wed Feb 20 10:48:59 2002 |
| Workbook: Case (Main) | | | |
| Material Streams | | | |
| Name | Feed | Products | |
| Vapour Fraction | 1.0000 | 1.0000 | |
| Temperature (K) | 880.0 * | 880.0 * | |
| Pressure (bar) | 1.378 * | 1.378 | |
| Molar Flow (gmole/s) | 152.2 * | 304.1 | |
| Mass Flow (kg/h) | 5.817e+004 | 5.817e+004 | |
| Liquid Volume Flow (m ³ /h) | 66.86 | 78.58 | |
| Heat Flow (kJ/h) | 8.826e+007 | 1.562e+008 | |
| Compositions | | | |
| Name | Feed | Products | |
| Comp Molar Flow (E-Benzenes) (gmole/s) | 152.2000 * | 0.3391 | |
| Comp Molar Flow (Styrene) (gmole/s) | 0.0000 * | 151.8628 | |
| Comp Molar Flow (Hydrogen) (gmole/s) | 0.0000 * | 151.8628 | |
| Energy Streams | | | |
| Name | Heat Duty | | |
| Heat Flow (kJ/h) | 6.791e+007 | | |
| Unit Ops | | | |
| Operation Name | Operation Type | Feeds | Products |
| PFR-100 | Plug Flow Reactor | Feed | Products |
| | | | Heat Duty |
| | | | Ignored |
| | | | Calc. Level |
| | | | No |
| | | | 500.0 * |

